

# ***B* Physics at the Tevatron and the *B* Factories**

**$\sin 2\beta$  and  $B_s$  Mixing  
Lecture II**

**Christoph Paus**  
*Massachusetts Institute of Technology*

XXXI International Meeting on Fundamental Physics

Soto de Cangas (Asturias), Spain  
February 24-28, 2003

# Overview

---

## Motivation and History

- + Why is  $CP$  violation interesting?
- + First important  $B$  physics measurements

## Introduction to the Experimental Setup

- +  $b$  production mechanisms as motivation
- +  $B$  Factories versus Tevatron
- + BaBar/Belle versus CDF/DØ

## Two Stories into some Detail

- + Tools for the measurement
- + Observation of  $CP$  violation in  $B$  systems,  $\sin 2\beta$
- + How Tevatron will measure  $B_s$  mixing,  $\Delta m_s$

# Web Pointers

---

## The experiments

- + **Tevatron:** <http://www-cdf.fnal.gov/>, <http://www-d0.fnal.gov/>
- + **B Factories:** <http://www.slac.stanford.edu/BFROOT>, <http://belle.kek.jp/>

## Overview reports

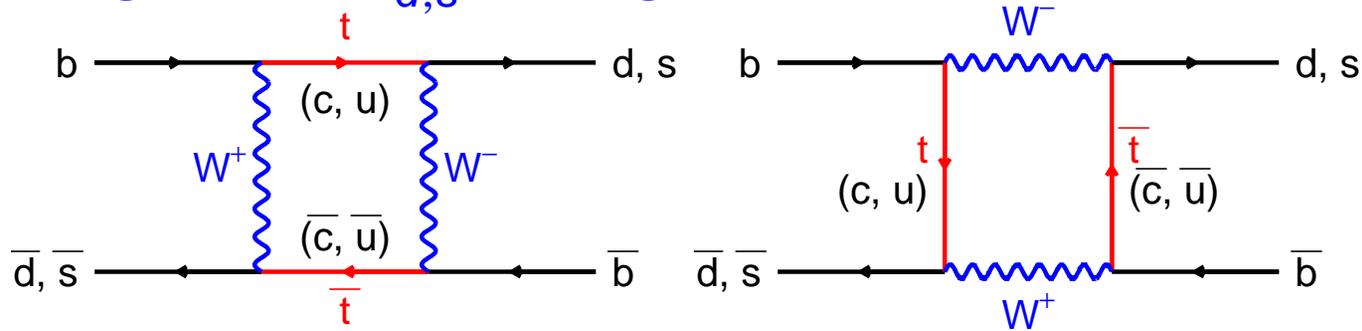
- + **The BaBar Physics Book**  
<http://www.slac.stanford.edu/pubs/slacreports/slac-r-504.html>
- + **B Physics at the Tevatron: Run II and Beyond**  
<http://arXiv.org/pdf/hep-ph/0201071>

## Excellent live videos / transparencies on the Web

- + **SLAC summer school 2002:**  
<http://www-conf.slac.stanford.edu/ssi/2002/>
- + **MIT Course: Heavy Flavor Physics (F. Würthwein)**  
<http://mit.fnal.gov/~fkw/teaching/mit8.881.html>

# Advanced Measurements: $B_s$ Mixing

Feynman diagram of  $B_{d,s}^0$  mixing:



## Differences

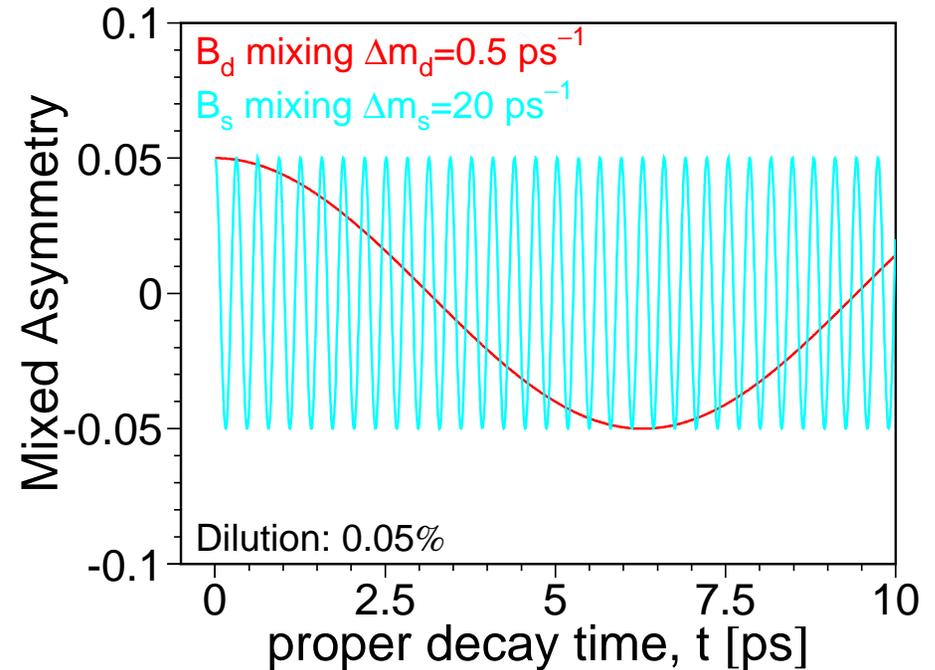
- +  $B_d^0$  crosses two families
- +  $B_s^0$  crosses one family
- + faster  $B_s^0$  mixing ( $\approx 40$ )

## Experimental challenge

- +  $ct$  resolution critical
- + fully hadronic decays:



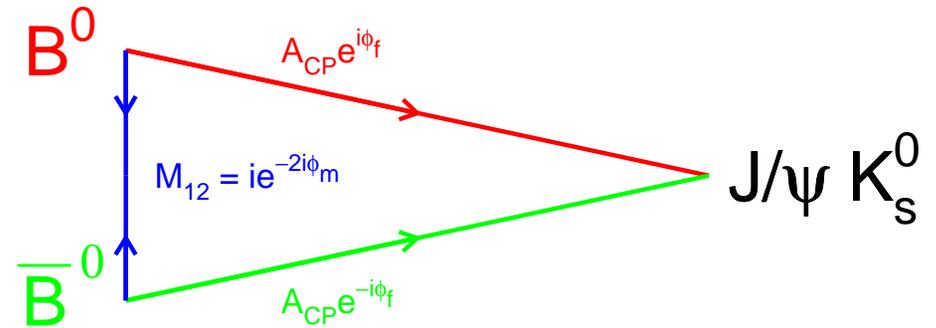
To be done at Tevatron



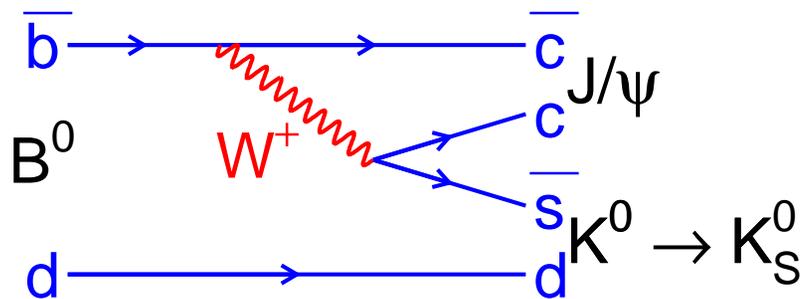
# Advanced Measurements: $CP$ Violation – $\sin 2\beta$

## $CP$ Violation mechanisms

- + interference of decay amplitudes
- + interference of mixing diagram
- + interference between mixing and decay amplitude



## Golden mode: $B^0 \rightarrow J/\psi K_S$



## $CP$ eigenstate: $\eta_{f_{CP}} = -1$

$$\begin{aligned} \text{Im} \lambda_{b \rightarrow c\bar{c}s} &= \eta_{f_{CP}} \text{Im} \left[ \frac{V_{tb} V_{td}^*}{V_{tb}^* V_{td}} \frac{V_{cb} V_{cs}^*}{V_{cb}^* V_{cs}} \frac{V_{cd}^* V_{cs}}{V_{cd} V_{cs}^*} \right] \\ &= \eta_{f_{CP}} \sin 2\beta \end{aligned}$$

$$A_{f_{CP}}(t) = \frac{\Gamma(\bar{B}^0(t) \rightarrow f_{CP}) - \Gamma(B^0(t) \rightarrow f_{CP})}{\Gamma(\bar{B}^0(t) \rightarrow f_{CP}) + \Gamma(B^0(t) \rightarrow f_{CP})} = -\text{Im} \lambda_{f_{CP}} \sin \Delta m_d t$$

# CKM Measurements from $B$

## Unitarity triangle and what measures it

### CP Violation parameter, $\sin 2\beta$

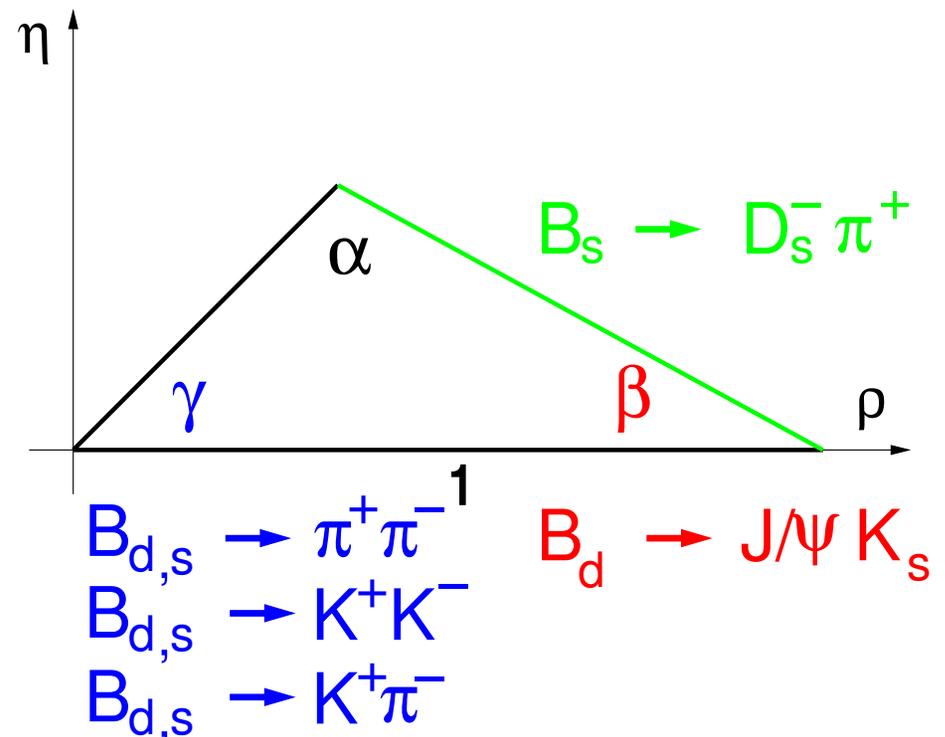
- +  $B^0 \rightarrow J/\psi K_S$
- + simple signature
- + relatively large branching

### Mixing parameter, $\Delta m_s$

- +  $B_S^0 \rightarrow D_S^- \pi^+$
- + needs hadronic trigger
- + clean signature
- + relatively large branching

### CP Violation parameter, $\gamma$

- +  $B_{S,d}^0 \rightarrow \pi\pi, K\pi, KK$
- + tricky.. for later



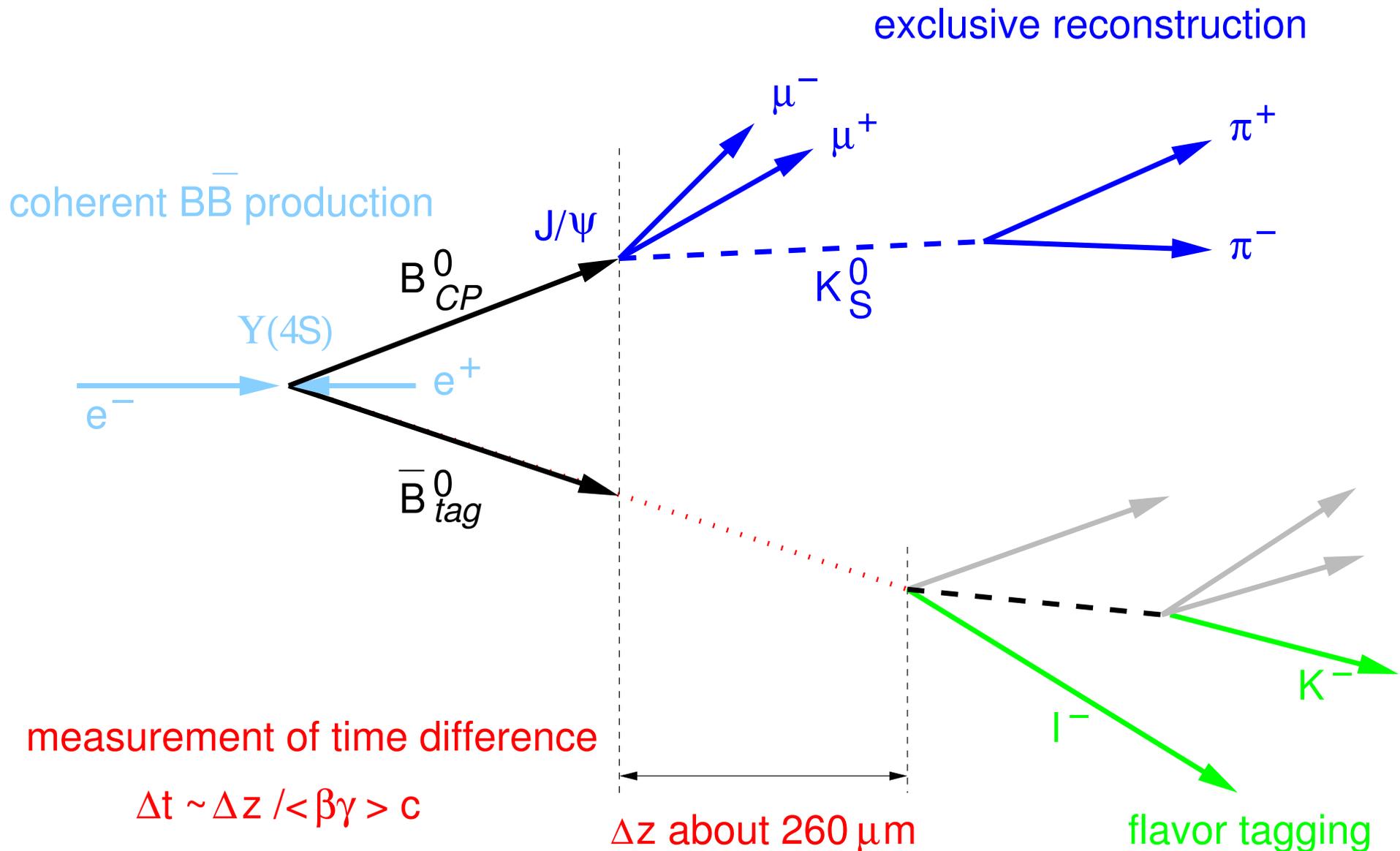
# Comparisons of $B$ Experiments

Accelerator	CESR,DORIS	LEP,SLC	PEP-II,KEKB	Tevatron
Detector	Argus,CLEO	ADLO,SLD	BaBar,Belle	CDF,DØ
$\sigma(b\bar{b})$	$\approx 1$ nb	$\approx 6$ nb	$\approx 1$ nb	$\approx 50$ $\mu$ b
$\sigma(b\bar{b}) : \sigma(had)$	0.26	0.22	0.26	0.001
$b$ hadrons	$B^0, B^+$	all	$B^0, B^+$	all
Boost $\langle \beta\gamma \rangle$	0.06	6	$\approx 0.5$	2-4
Production	$B$ s at rest	$b\bar{b}$ btb	forward boost	$b\bar{b}$ not btb
Event pile-up	no	no	no	yes
Trigger	inclusive	inclusive	inclusive	selective

## Comments

- + experimentally LEP/SLC at  $Z$  looks ideal – but expensive
- + Babar and Belle can cheaply produce although not all
- + Tevatron has the highest cross section and can do all but lots of background
- + nice complementary setup

# Detailed Cartoon of Measurement at $\Upsilon(4S)$



# Analysis Components

---

**Final State Reconstruction**

**Measurement of  $t$  or  $\Delta t$**

**$b$  Flavor Tagging**

---

# Final State Reconstruction

# Main $B$ Reconstruction Variables – $\Upsilon(4S)$

In  $\Upsilon(4S)$  rest frame:

$E_{beam}^*$  – beam energy

$(E_B^*, p_B^*)$  –  $B$  four momentum

Two almost uncorrelated variables

$$+ \Delta E = E_B^* - E_{beam}^* \quad \text{signal at } \Delta E \approx 0$$

$$+ m_{ES} = \sqrt{E_{beam}^{*2} - p_B^{*2}} \quad \text{signal at } m_{ES} \approx m_B$$

Energy substituted mass  $m_{ES}$ :  $E_{beam}$  replaces  $E_B$

Resolutions

$$+ \sigma_{\Delta E}^2 = \sigma_{beam}^2 + \sigma_E \approx \sigma_E \approx 10 - 40 \text{ MeV}$$

$$+ \sigma_{m_{ES}}^2 = \sigma_{beam}^2 + \frac{p^2}{m_B^2} \sigma_p^2 \approx \sigma_{beam}^2 \approx 2.6 \text{ MeV}$$

# Main $B$ Reconstruction Variables – $\Upsilon(4S)$

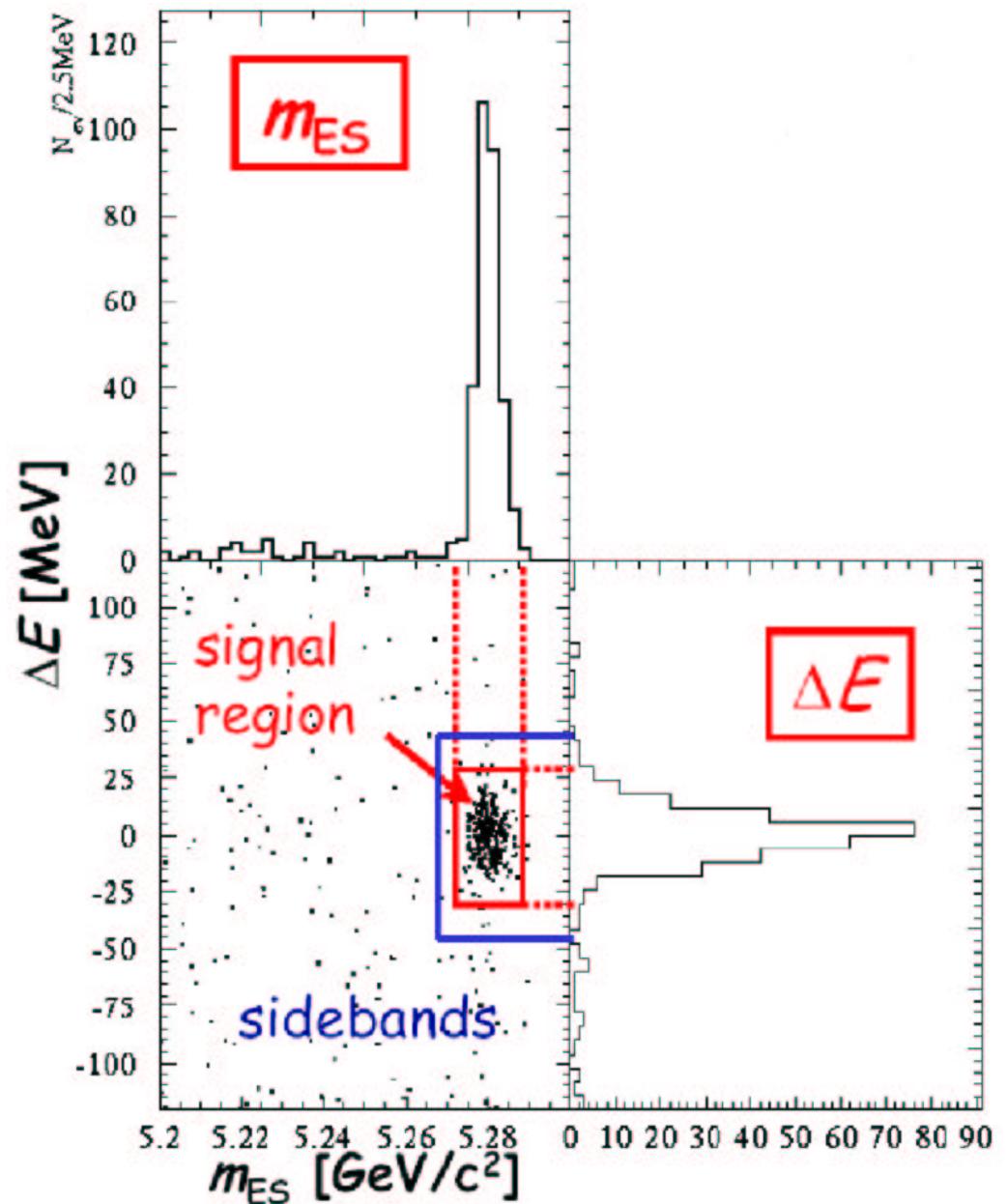
Channel:  $B^0 \rightarrow J/\psi K_S^0$

Signal region

+  $\pm 3\sigma$  in  $m_{ES}$  and  $\Delta E$

Sideband region

+ rest window for bg

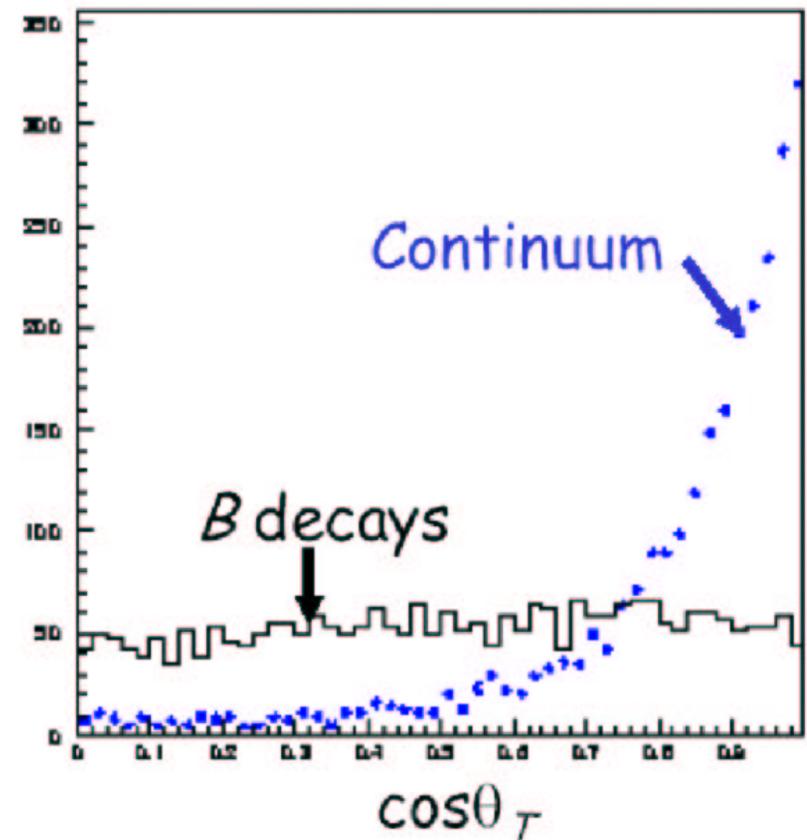
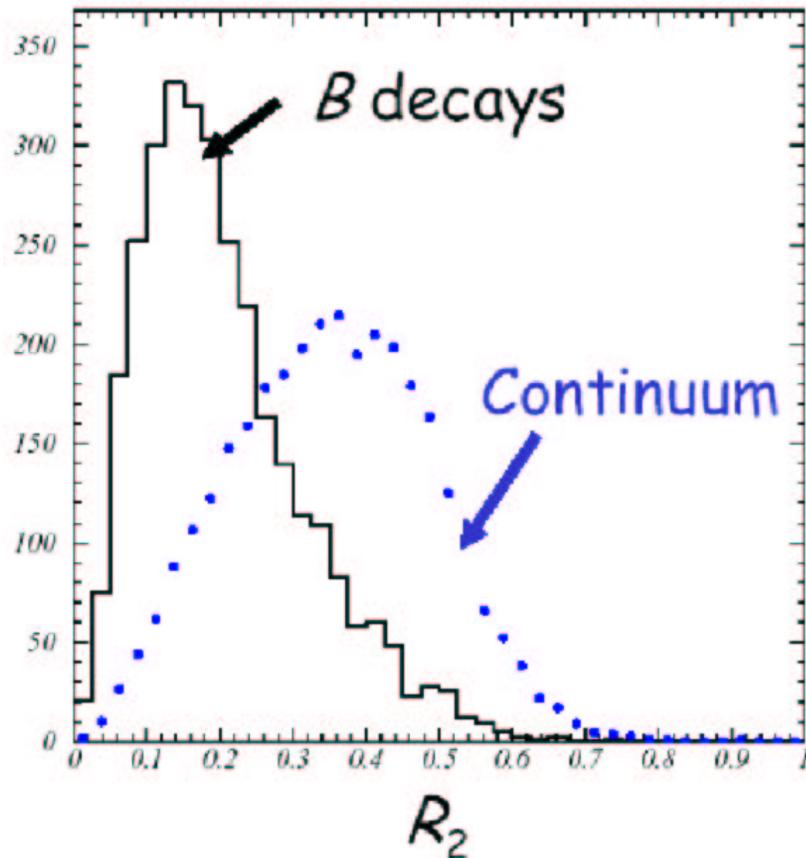


# Continuum Background Suppression – $\Upsilon(4S)$

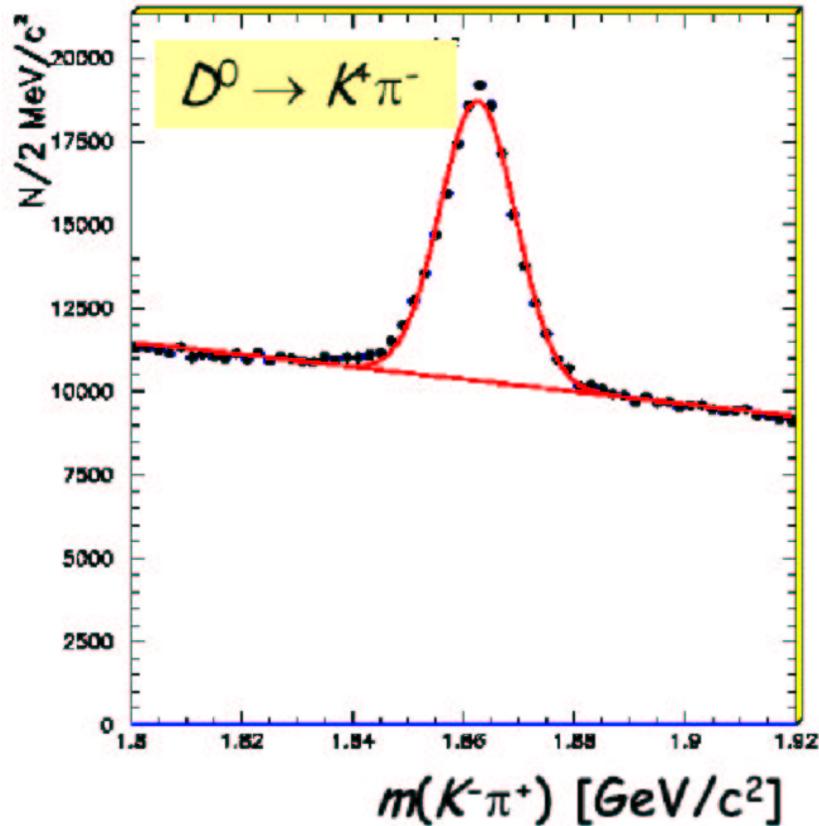
Main Idea:  $B\bar{B}$  is spherical in  $\Upsilon(4S)$  CM since produced at rest  
Continuum background is jet-like

Ratio of 2<sup>nd</sup>/0<sup>th</sup> Fox-Wolfram moments

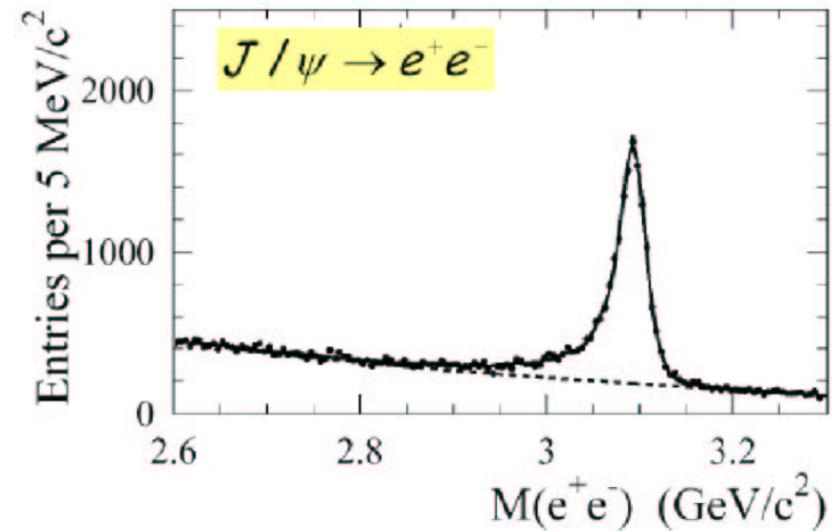
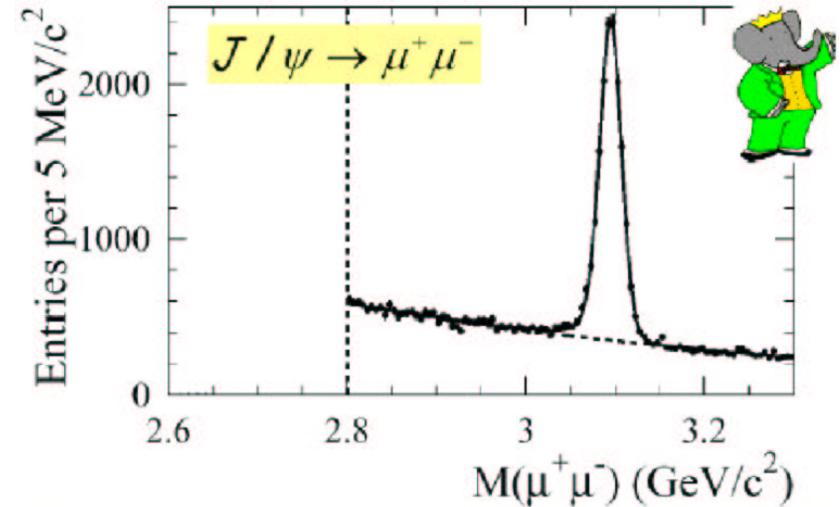
Angle of thrust axis of *rest* wrt  $B$  candidate direction  $\theta_T$



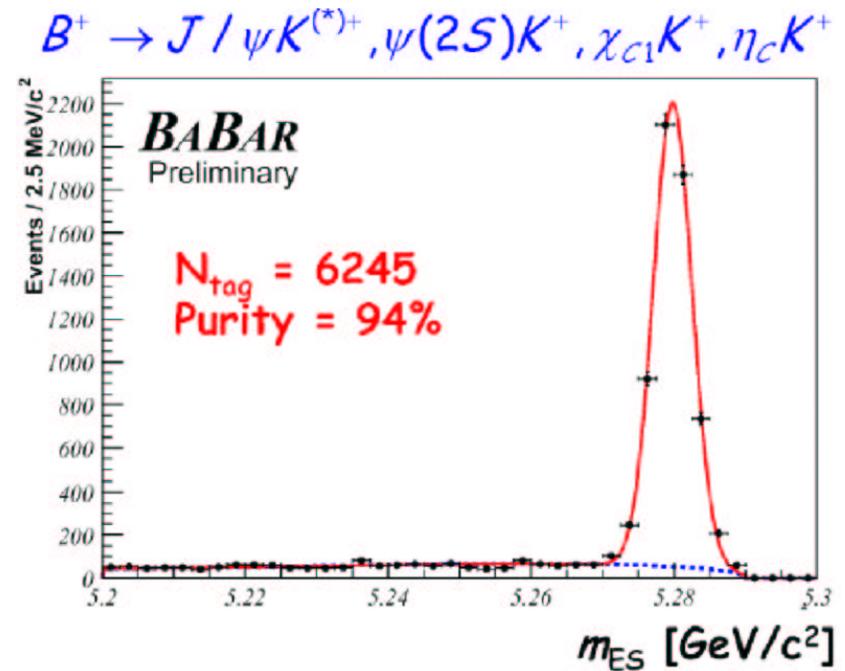
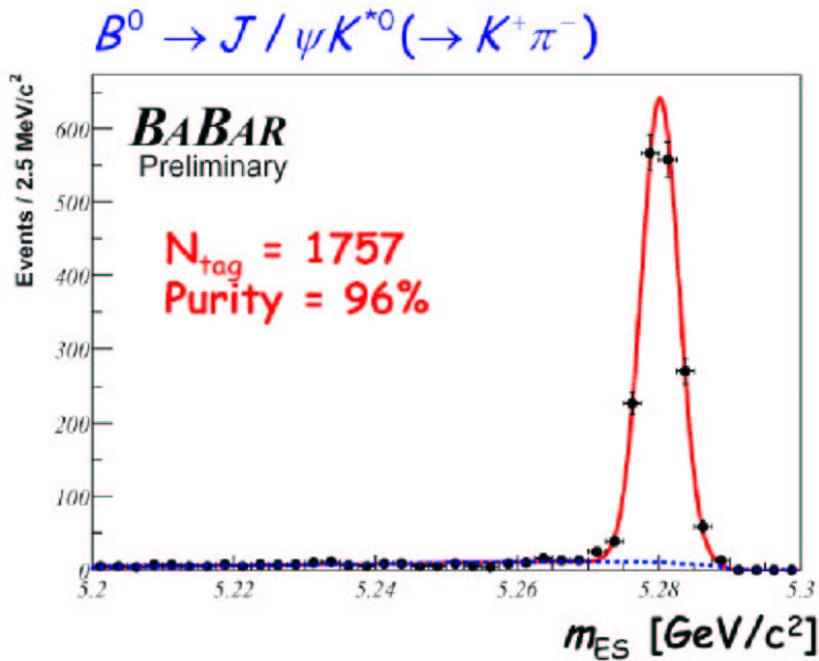
# Subresonances – $\Upsilon(4S)$



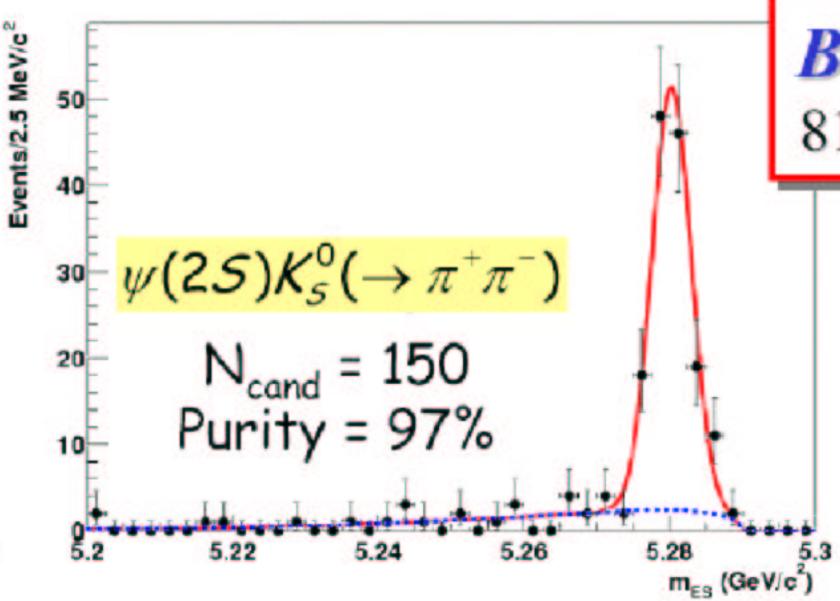
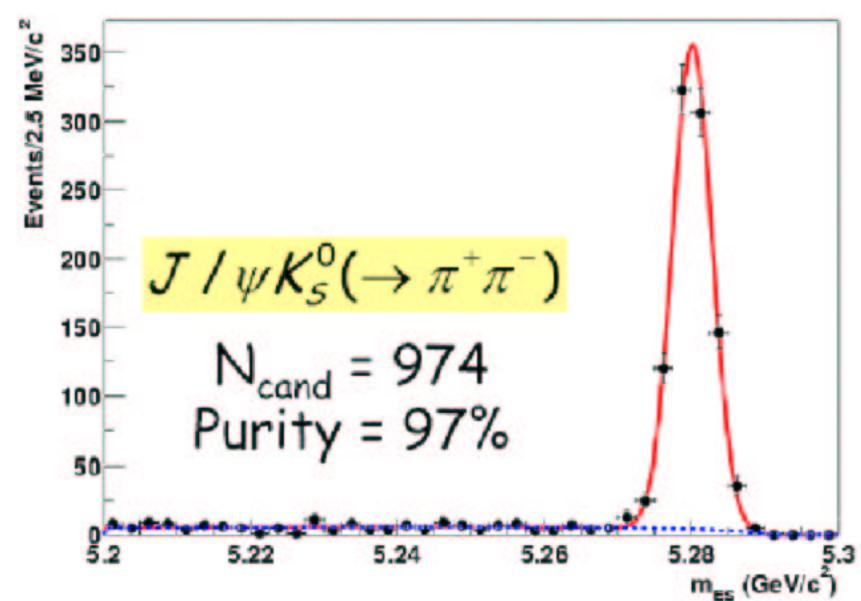
masses are constraint after selection



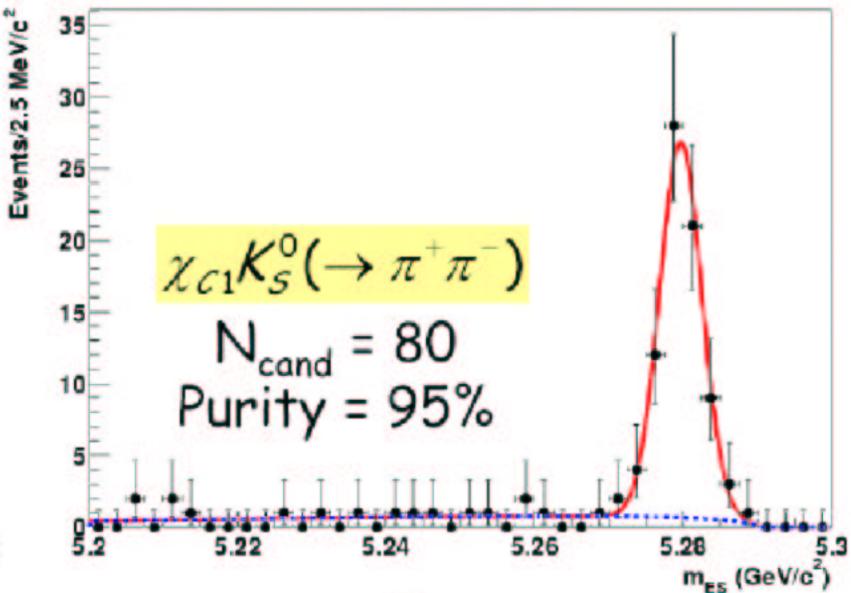
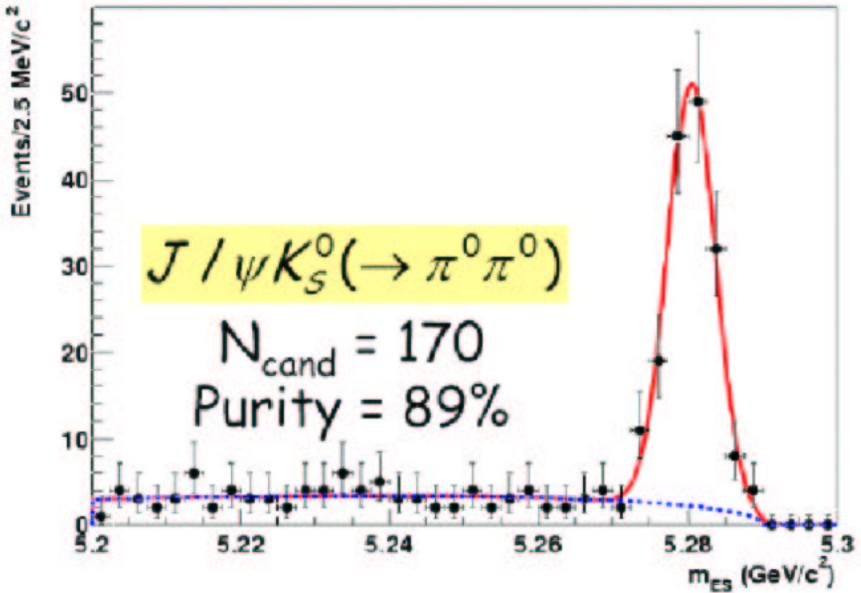
# Hadronic Samples at $\Upsilon(4S)$ – Self-Tagging



# Hadronic Samples at $\Upsilon(4S)$ – $CP$ Eigenstate



**BABAR**  
81.3 fb<sup>-1</sup>



Candidates & purity for  $m_{ES} > 5.27 \text{ GeV}/c^2$

# Reconstruction of $b$ Hadrons at Tevatron

---

No knowledge of total energy of collision

Basically no constraints on energy or momentum

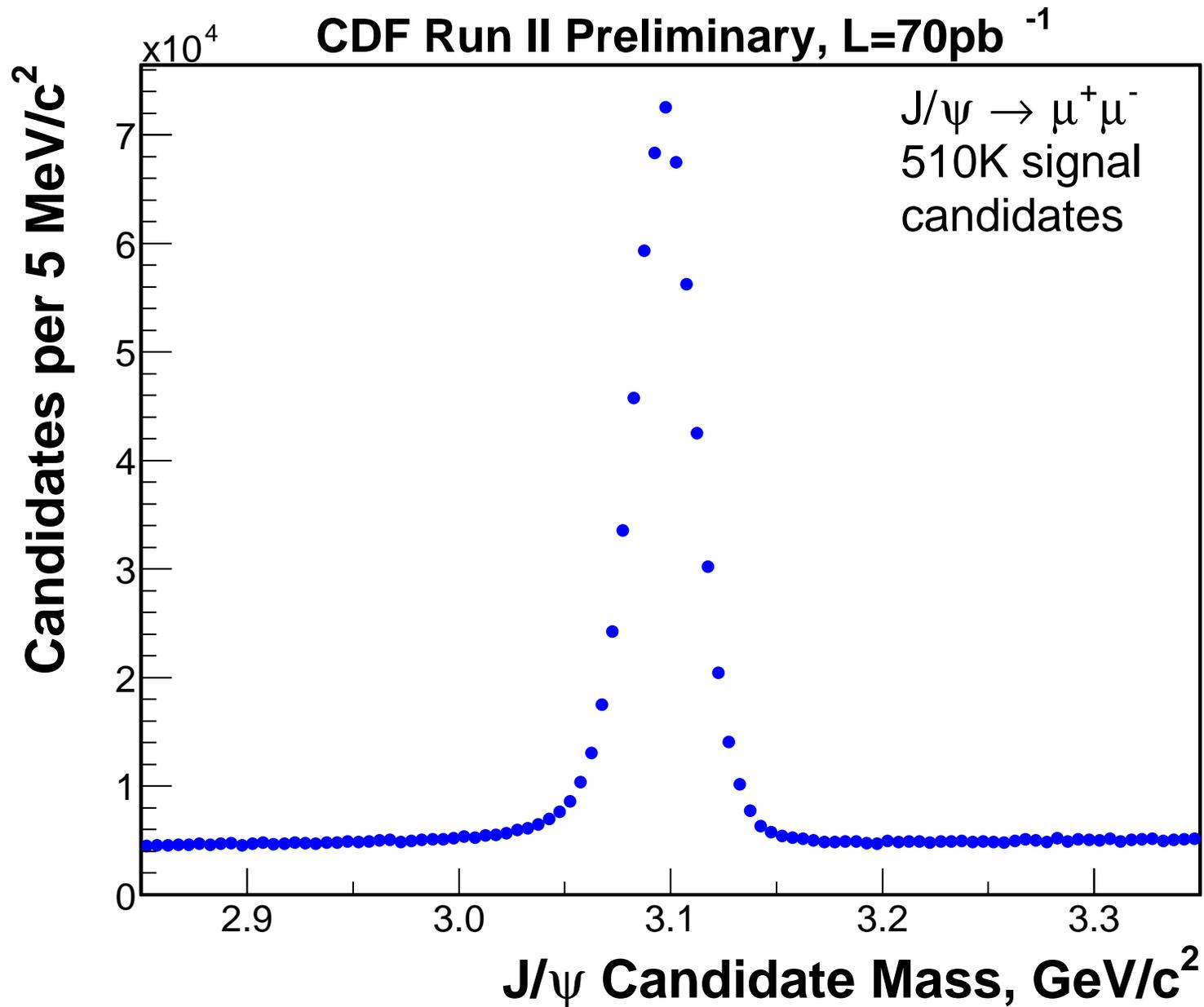
Use high  $p_T$  leptons

Use high  $p_T$  resonances

Use precise knowledge of vertex positions

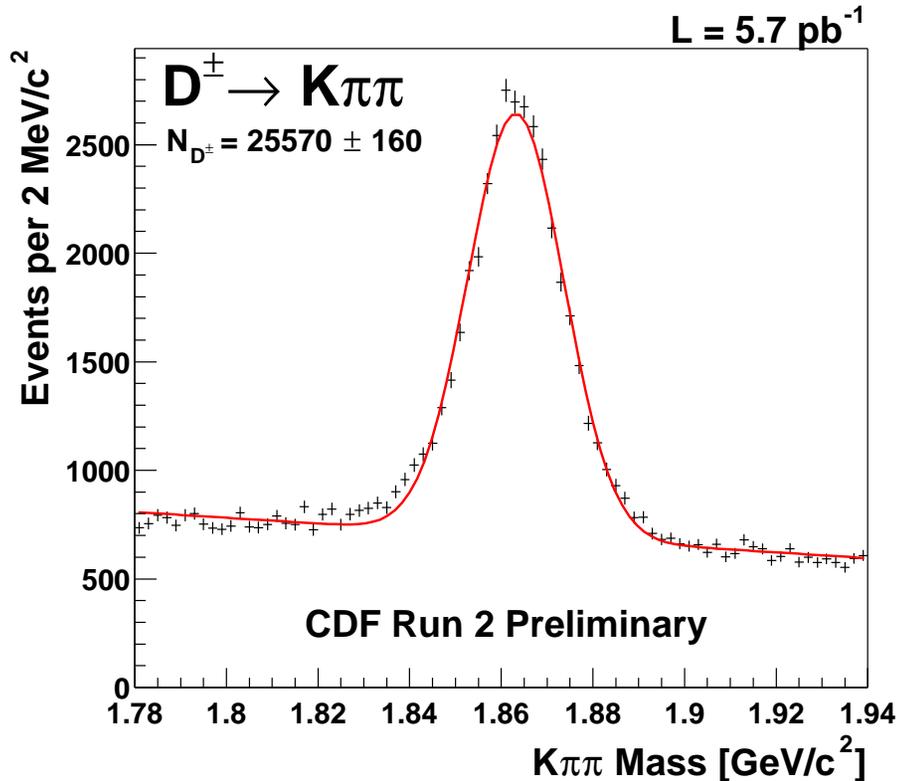
- + require  $b$  hadron to point at primary vertex
- + require  $L_{xy} > 0$  typically  $100 \mu\text{m}$  (careful: bias  $ct$ )

# Subresonances at CDF – $J/\psi$

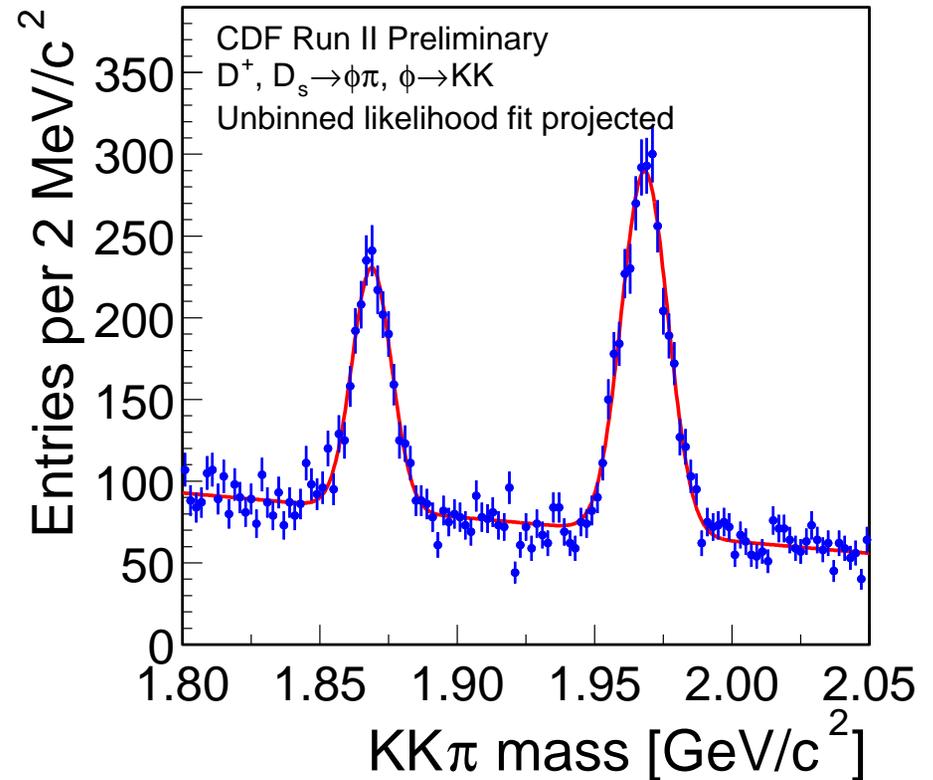


# Subresonances at CDF – Charm

Result of displaced track trigger!!  
No Lepton was harmed in making these plots

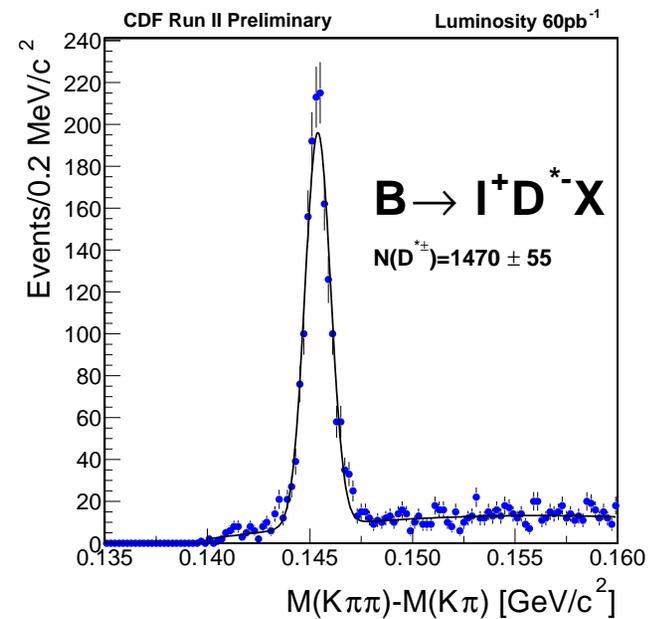
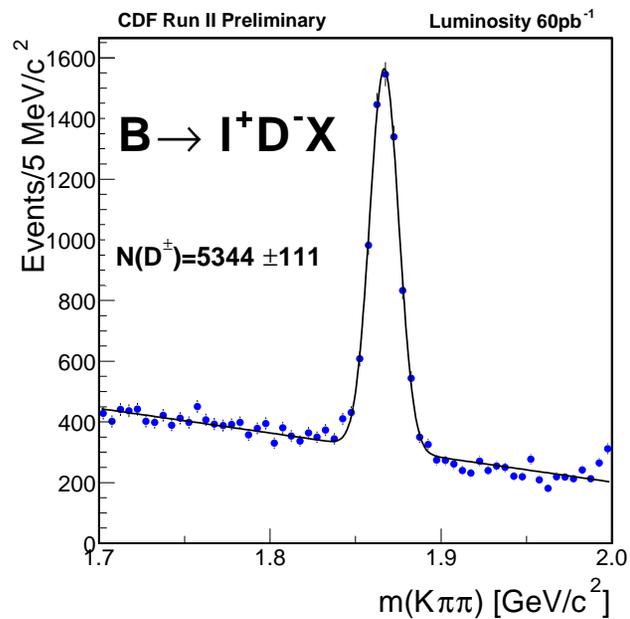
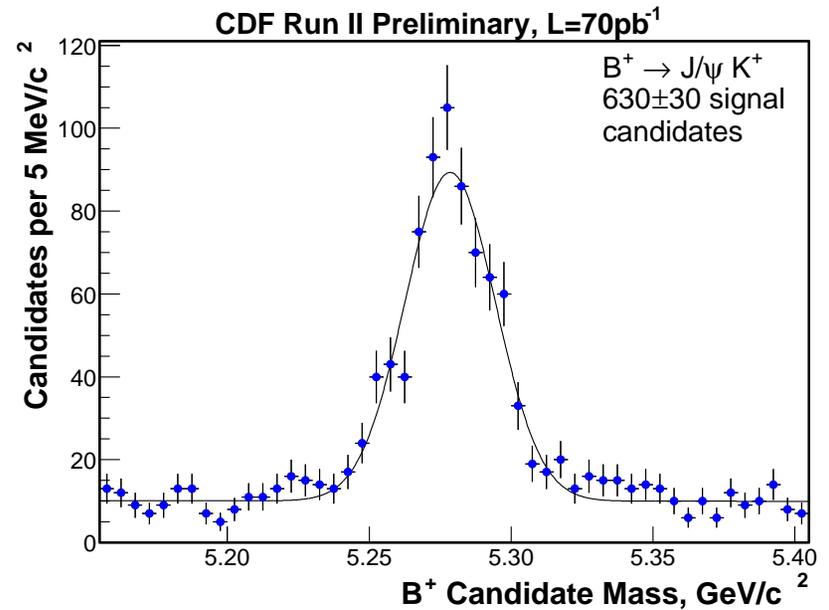
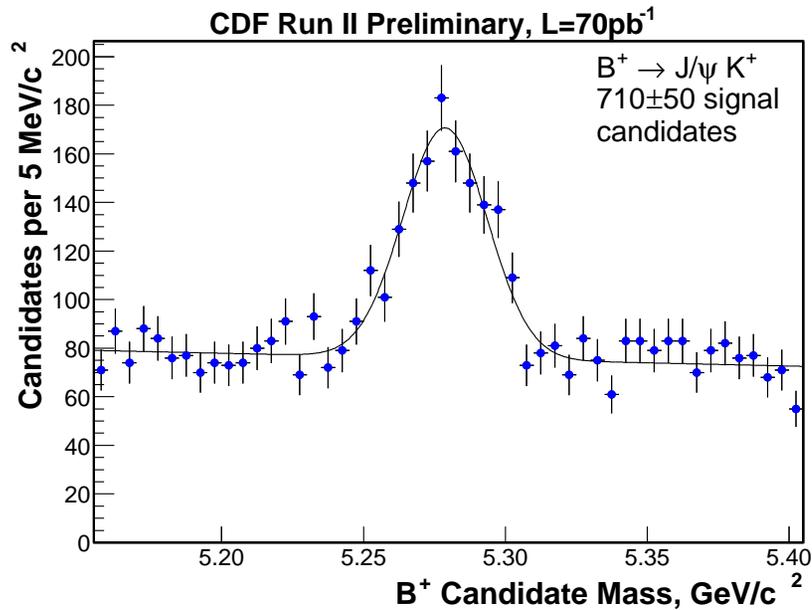


20 times more data available



used to measure mass difference

# Self Tagging Final States at CDF

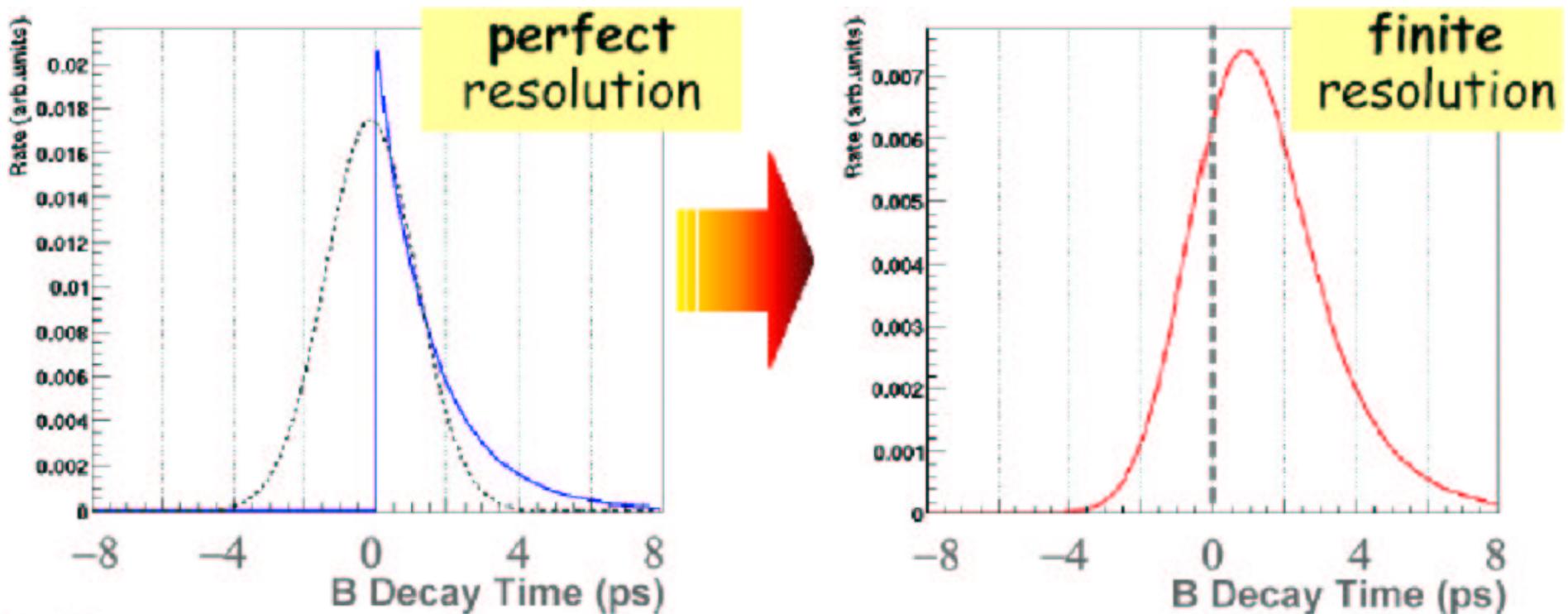


---

# Measurement of $t$ or $\Delta t$

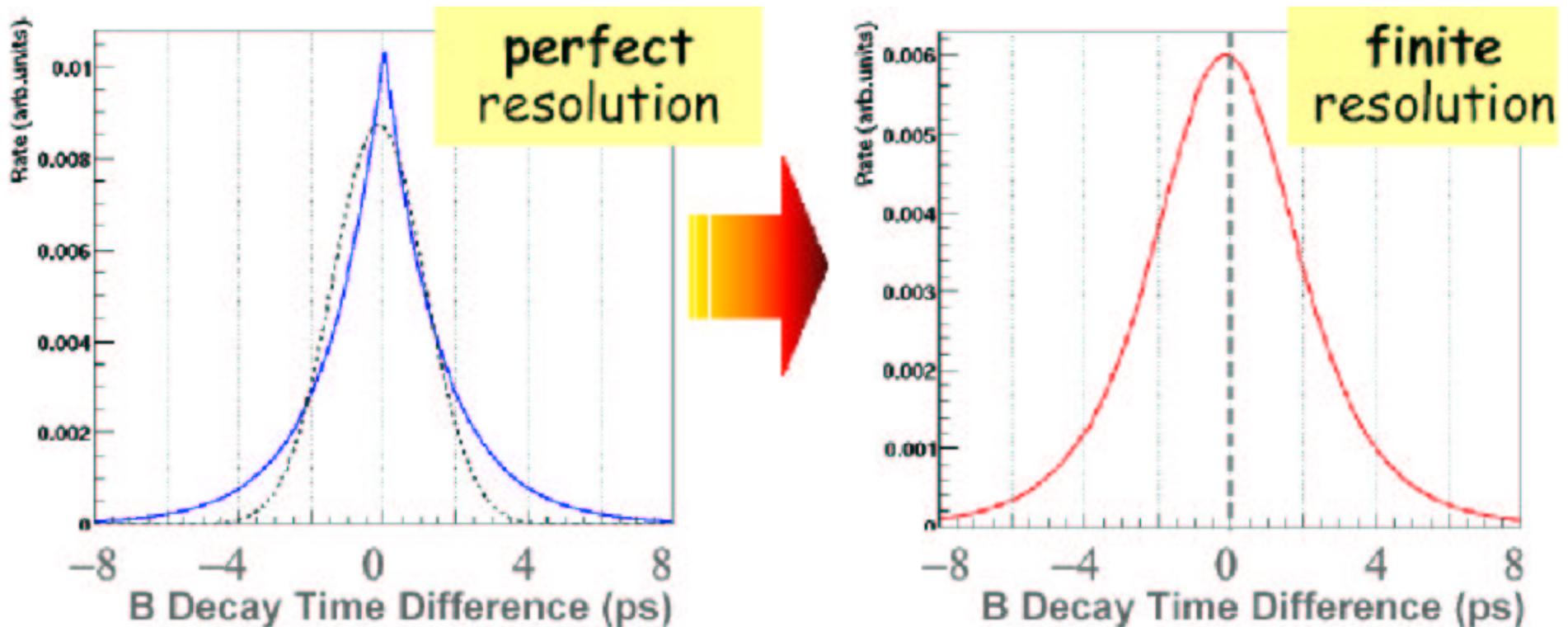
# Measurement of $t$ at Tevatron/LEP

Primary vertex is well known point  
Negative tails allow to control resolution function



# Measurement of $\Delta t$ at B Factories

Determine  $\Delta t$  from  $\Delta z$  between  $B$  Mesons  
Resolution function and lifetime are convoluted



# B Lifetime Measurements at B Factories

BaBar ( $20.7 \text{ fb}^{-1}$ )

PRL 87 (2001) 201803

$$\tau_{B^0} = 1.546 \pm 0.032 \pm 0.022 \text{ ps}$$

$$\tau_{B^+} = 1.673 \pm 0.032 \pm 0.023 \text{ ps}$$

$$\tau_{B^+}/\tau_{B^0} = 1.082 \pm 0.026 \pm 0.012$$

Belle ( $29.1 \text{ fb}^{-1}$ )

PRL 88 (2002) 171801

$$\tau_{B^0} = 1.554 \pm 0.030 \pm 0.019 \text{ ps}$$

$$\tau_{B^+} = 1.673 \pm 0.026 \pm 0.015 \text{ ps}$$

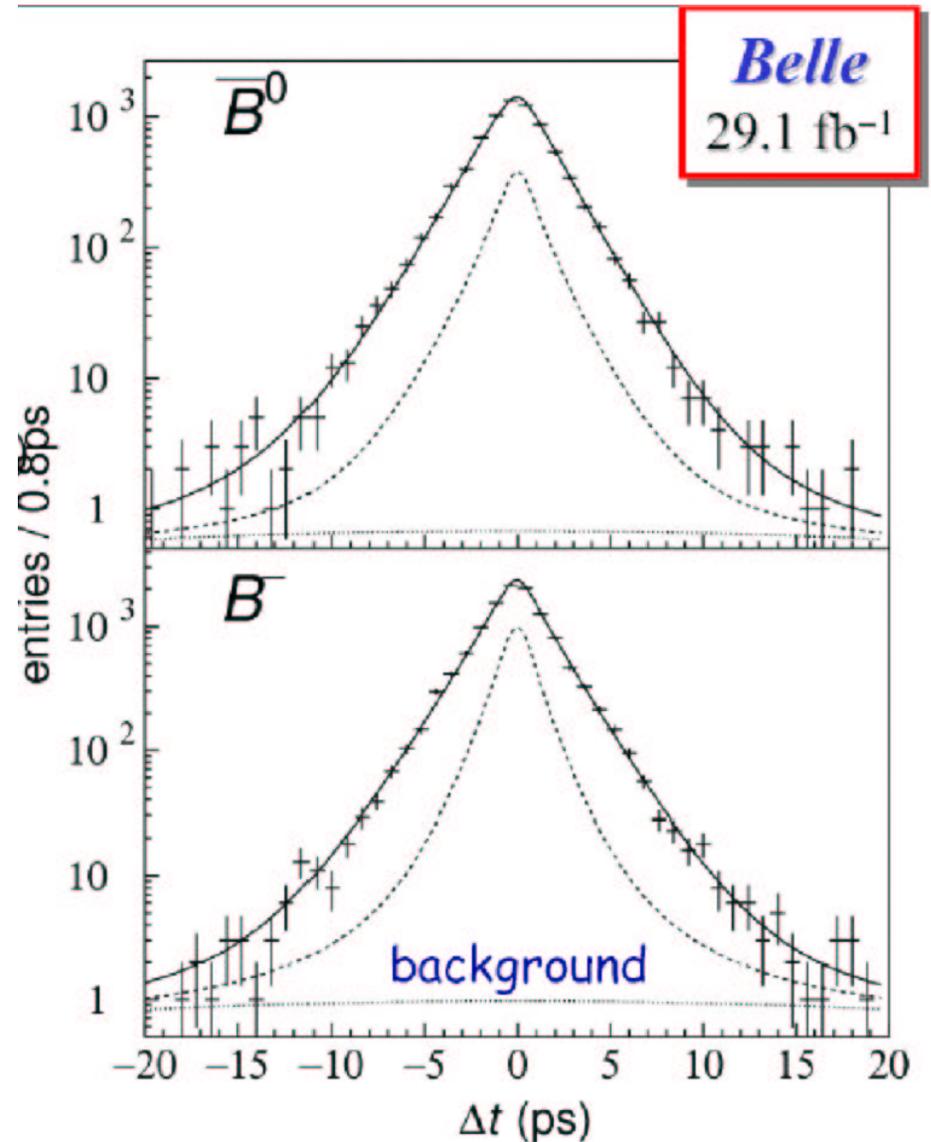
$$\tau_{B^+}/\tau_{B^0} = 1.091 \pm 0.023 \pm 0.014$$

Agree within each other

Agree with world average

Proof of principle:

Control resolution function



# B Lifetime Measurements at Tevatron

Large sample of  $J/\psi \rightarrow \mu^+\mu^-$  events

- + calibrate resolution
- + understand alignment
- + measure inclusive  $B$  lifetime
- + so far only  $r$ - $\phi$  silicon used

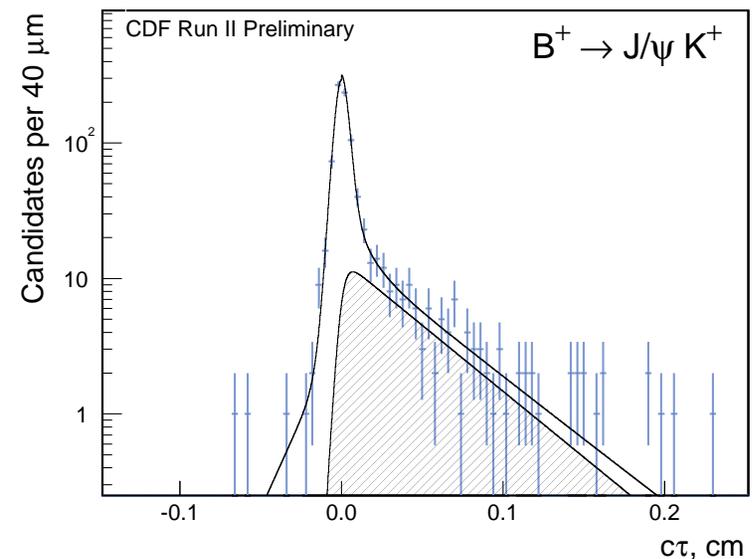
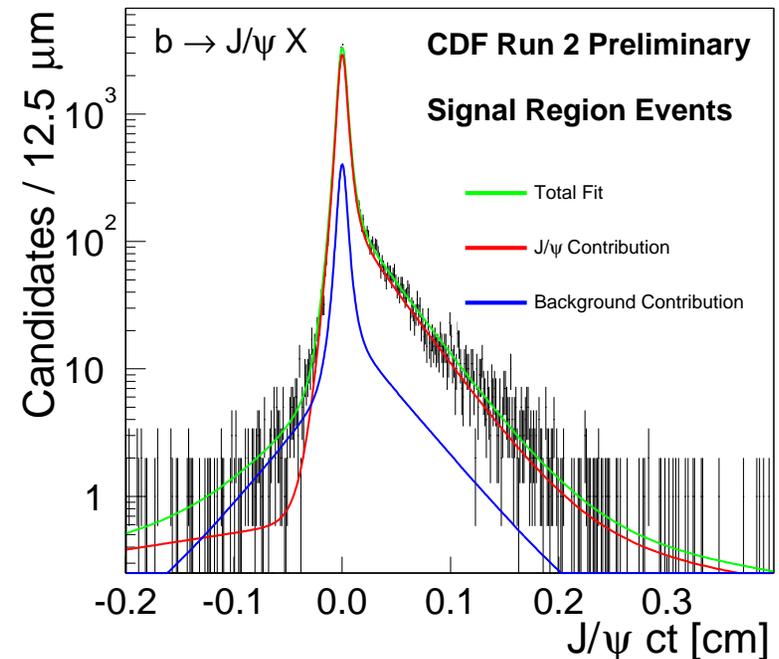
Lifetime measurements

$$c\tau_{incl} = 458 \pm 10_{(stat)} \pm 11_{(sys)} \mu\text{m}$$

$$c\tau_{B^+} = 446 \pm 43_{(stat)} \pm 13_{(sys)} \mu\text{m}$$

About CDF results

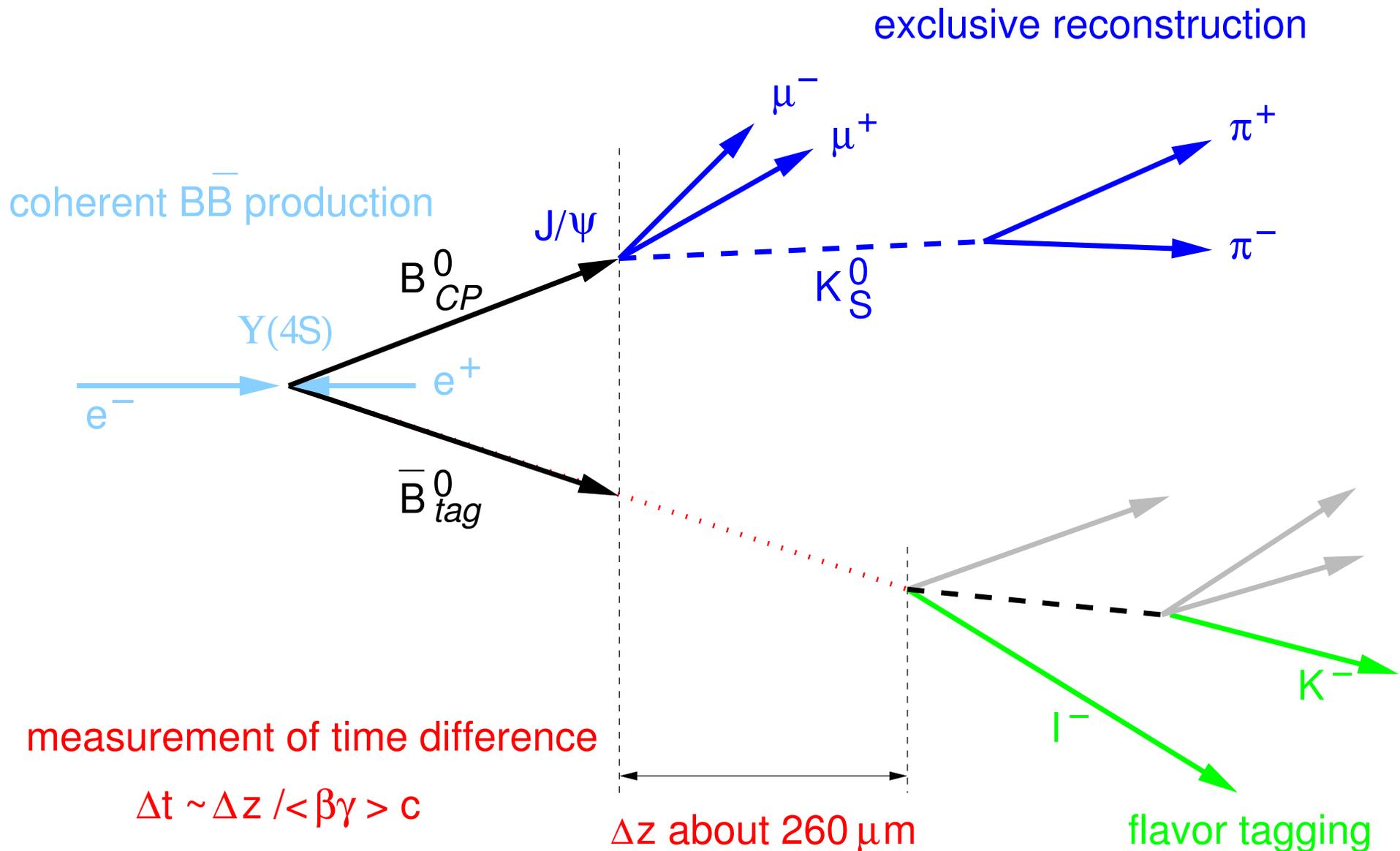
- + silicon already well understood
- + consistent with Run 1, world average
- + incl. systematics as Run 1
- + major improvements expected:  
Layer 00, 3D tracking, alignments
- + now ten times more data
- + very soon  $\tau_{B_s}$  and  $\tau_{\Lambda_b}$



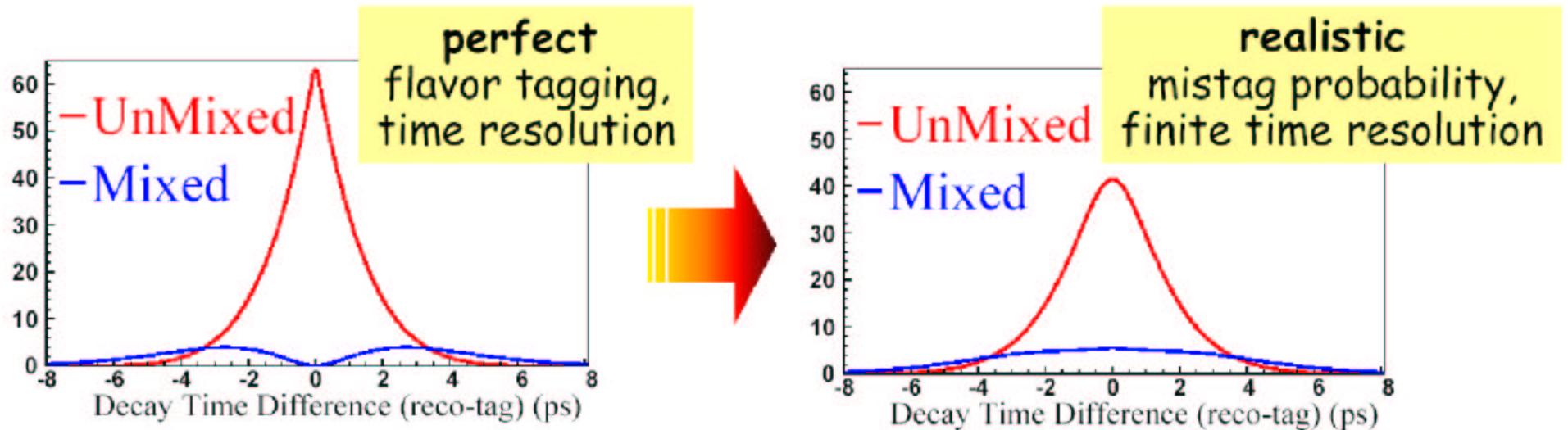
---

# ***b* Flavor Tagging**

# Detailed Cartoon of Measurement at $\Upsilon(4S)$



# Distribution of Mixing at $\Upsilon(4S)$



## Distribution of mixed and unmixed events

$$f_{mix,\pm}(\Delta t) = \left[ \frac{e^{-|\Delta t|/\tau_B}}{4\tau_B} (1 \pm (1 - 2w)\cos\Delta m_d \Delta t) \right] \otimes R(\Delta t)$$

$f_{mix,+}$  - means unmixed or different flavors

$f_{mix,-}$  - means mixed or same flavors

$1 - 2w$  - quality of the tagging algorithm (dilution)

$R(\Delta t)$  - detector resolution function

# Methods of Flavor Tagging at $B$ Factories

At  $B$  factories flavor tags rely on *tagging* side

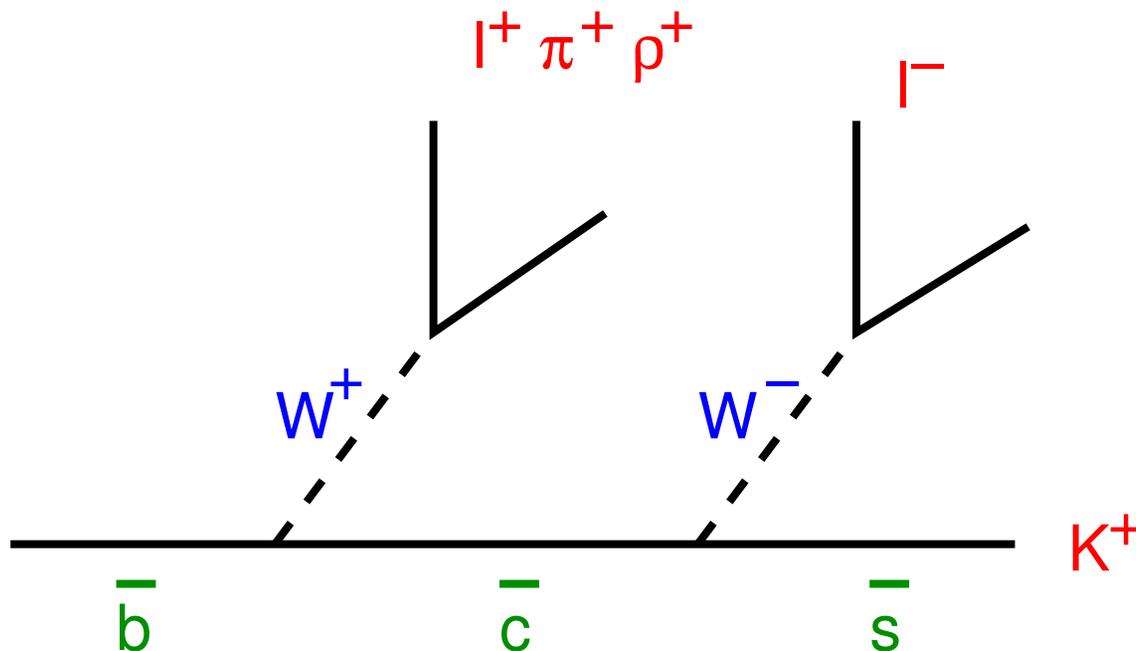
- + primary lepton
- + secondary lepton
- + Kaon(s)
- + Soft pions from  $D^*$  decays
- + Fast charged tracks

$$B^0 \rightarrow D^{*-} \ell^+ \nu$$

$$B^0 \rightarrow D^- \pi^+, D^- \rightarrow K^{*+} \ell^- \bar{\nu}$$

$$B^0 \rightarrow \bar{D} X, \bar{D} \rightarrow K^+ X$$

$$B^0 \rightarrow D^{*-} X, D^{*-} \rightarrow \bar{D}^0 \pi_S^-$$



# Flavor Tagging Performance at $B$ Factories – BaBar

Tagging Algorithm	efficiency	wrong tag $w$	$Q = \varepsilon(1 - 2w)^2$
Lepton	$10.9 \pm 0.3$	$9.0 \pm 1.4$	$7.4 \pm 0.5$
Kaon	$35.8 \pm 1.0$	$17.6 \pm 1.0$	$15.0 \pm 0.9$
NeuralNet 1	$7.7 \pm 0.2$	$22.0 \pm 2.1$	$2.5 \pm 0.4$
NeuralNet 2	$13.8 \pm 0.3$	$35.1 \pm 1.9$	$1.2 \pm 0.3$
Combined	$68.4 \pm 0.7\%$	$9.0 \pm 1.4\%$	$26.1 \pm 1.2\%$

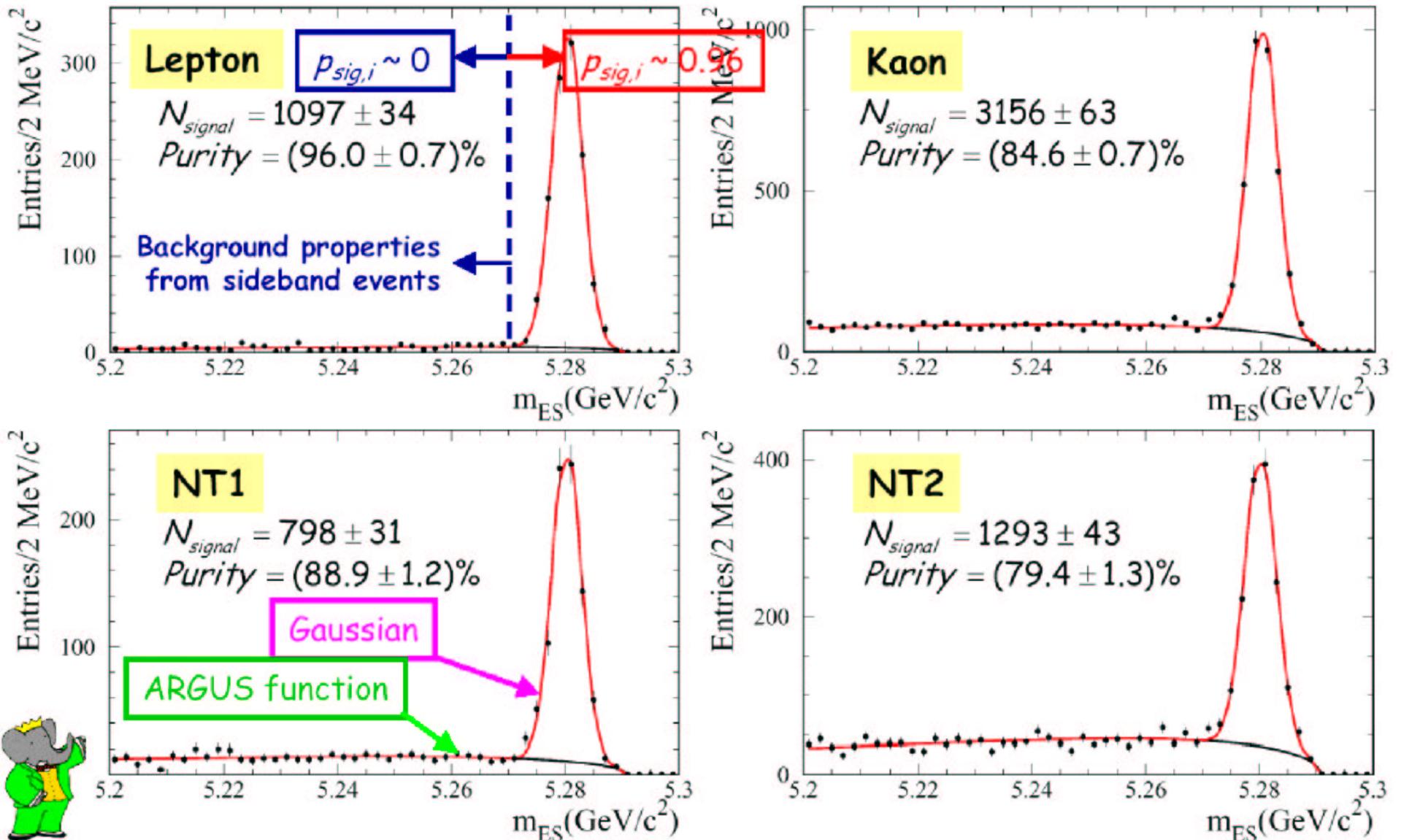
Large sample of fully reconstructed events allows precise measurement

Calibrate the taggers using data

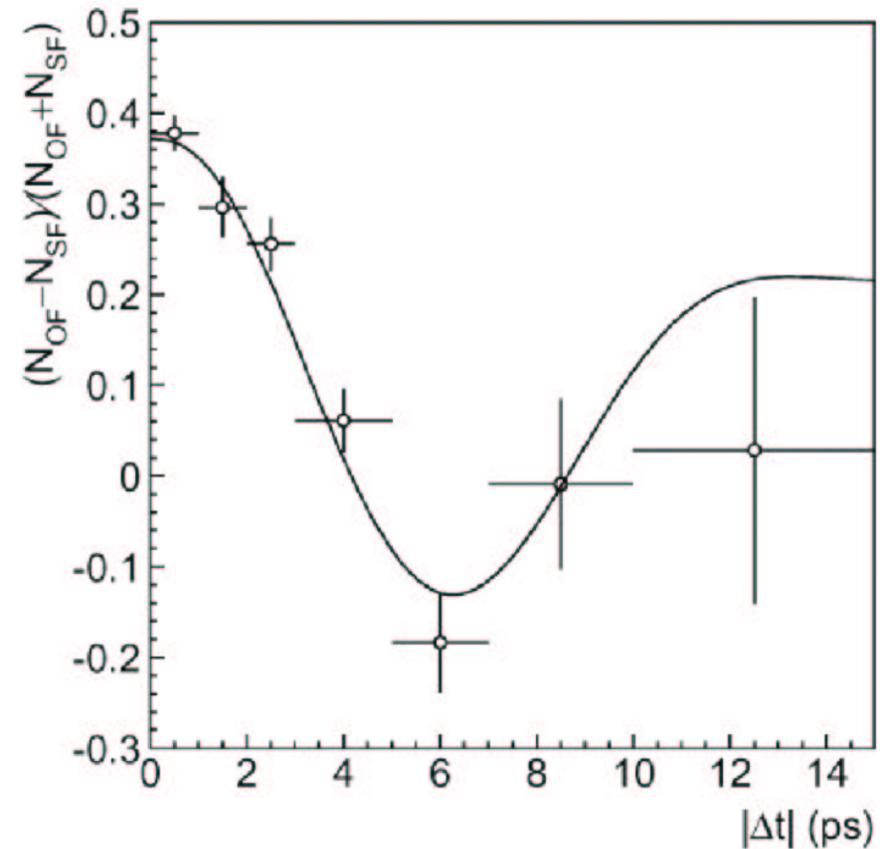
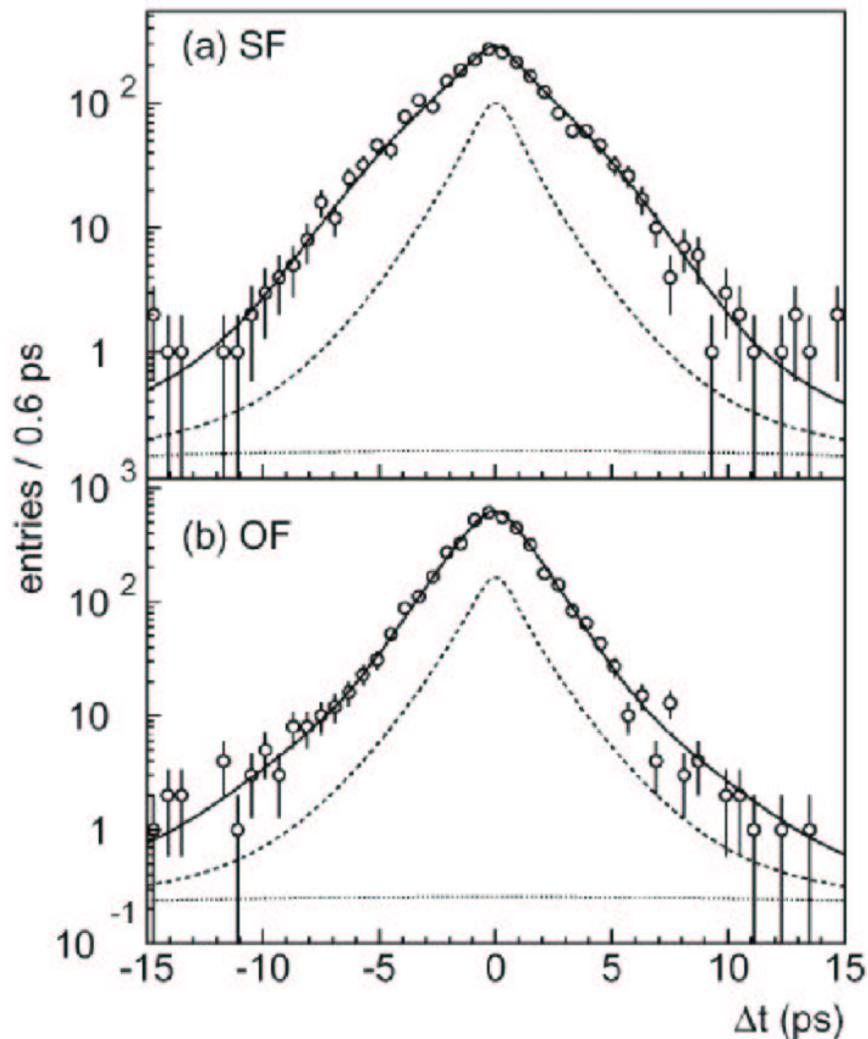
No MonteCarlo used here

Quality meter:  $\sigma(\sin 2\beta)_{stat} \propto 1/\sqrt{Q}$

# Event Samples for Mixing Measurement – BaBar



# Mixing Measurements – BaBar/Belle



**BELLE**  
29.1 fb<sup>-1</sup>

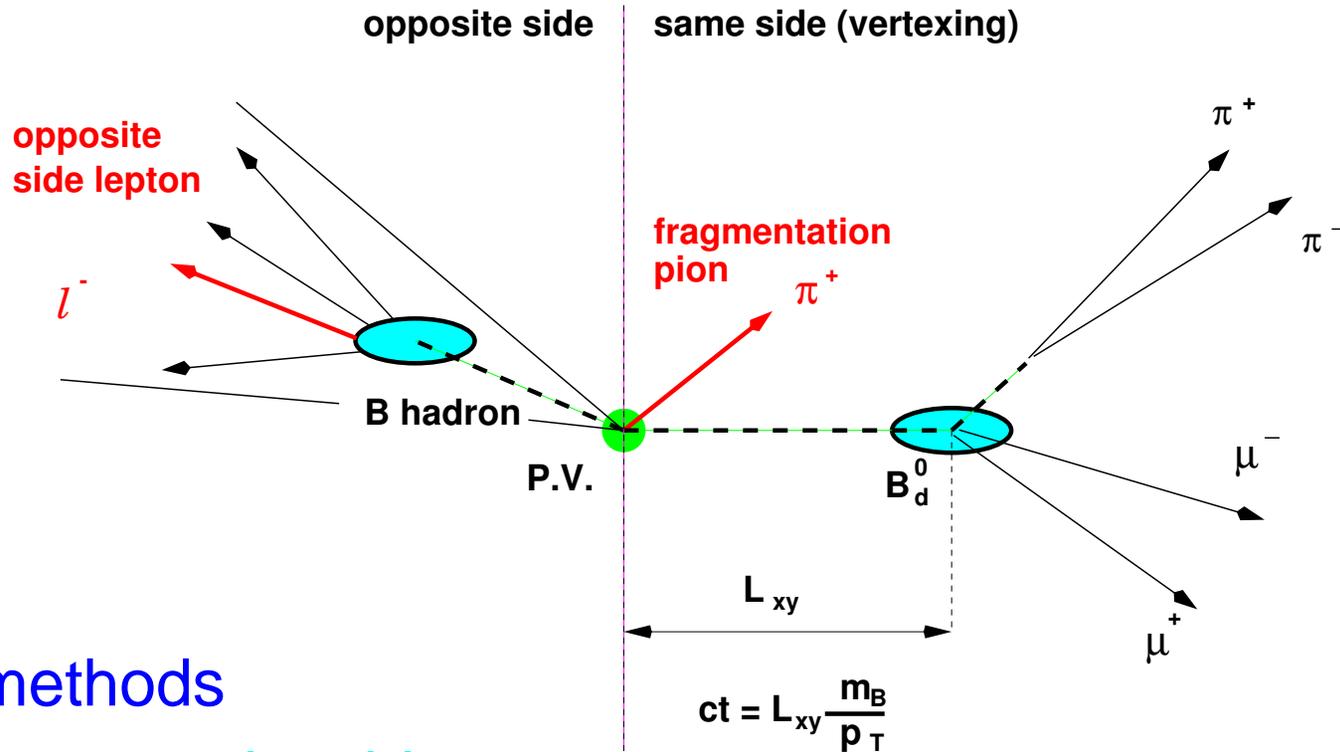
$$\Delta m_d = 0.528 \pm 0.017 \pm 0.011 \text{ ps}^{-1} \text{ (Belle)}$$

$$\Delta m_d = 0.516 \pm 0.016 \pm 0.010 \text{ ps}^{-1} \text{ (Babar)}$$

PRL 88 (2002) 221802

Ch. Paus, IMFP Feb 24-28, 2003 - 31

# Flavor Tagging at the Tevatron



## Tagging methods

- + lepton opposite side tag
- + kaon OS tag
- + jet charge OS tag
- + pion same side tag
- + kaon same side tag ( $B_s$ )

## Same side tagging



# Flavor Tagging at the Tevatron

Example: taggers for  $B^0 \rightarrow J/\psi K_S^0$

Method	$\varepsilon$	$D = 1 - 2w$	$\varepsilon D^2$
Lepton	$(5.6 \pm 1.8)\%$	$(62.5 \pm 14.6)\%$	$(2.2 \pm 1.2)\%$
Jet Charge	$(40.2 \pm 3.9)\%$	$(23.5 \pm 6.9)\%$	$(2.2 \pm 1.3)\%$
Same Side	$(\approx 70)\%$	$(\approx 17)\%$	$(2.1 \pm 0.5)\%$
Total			$(6.3 \pm 1.7)\%$

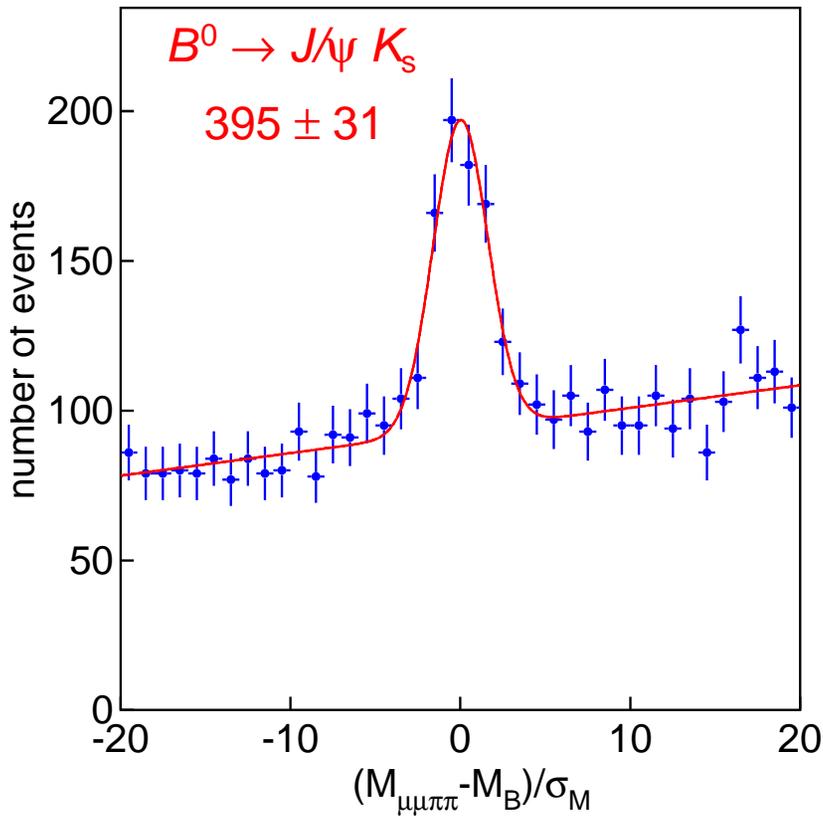
Tagger depend on kinematics of event sample: trigger bias  
Measure  $CP$  asymmetry,  $\sin 2\beta$

$$A_0(t) \equiv \frac{N(t)_{B^0 \rightarrow f_{CP}} - N(t)_{\overline{B^0} \rightarrow f_{CP}}}{N(t)_{B^0 \rightarrow f_{CP}} + N(t)_{\overline{B^0} \rightarrow f_{CP}}} = D \sin 2\beta \sin(\Delta m_q t)$$

For  $\sin 2\beta$ : measure Dilution  $(1 - 2w)$  first  $\rightarrow$  calibration sample

CDF used:  $B^0 \rightarrow J/\psi K^{*0}$  extrapolate different kinematics

# First $\sin 2\beta$ at CDF (1999)

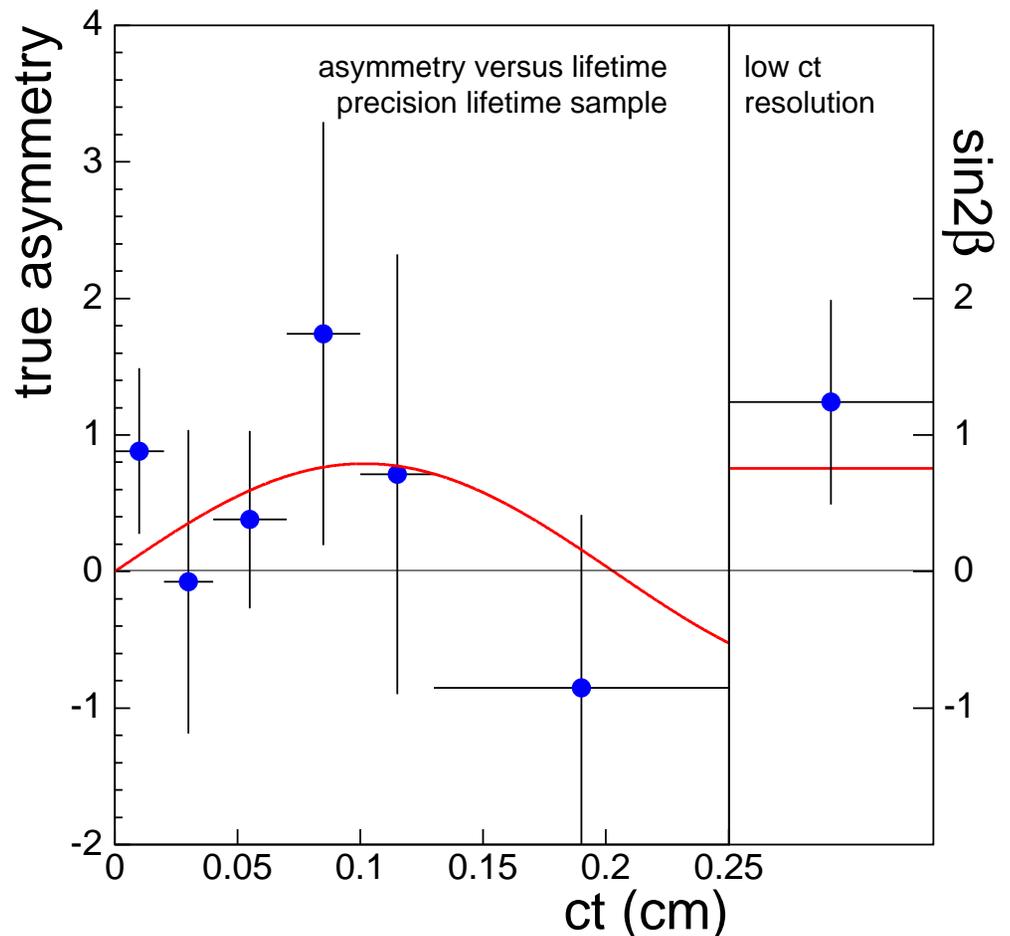


Same side  $\pi$ , jet charge and soft lepton

$$\sin 2\beta = 0.79^{+0.41}_{-0.44} \quad \epsilon D^2 = 6.3 \pm 1.7\%$$

first presented 1999: PRD 61 (2000) 072005

Not very clean but  $\approx 400$  events  
 No significant  $CP$  violation yet



# The real $\sin 2\beta$ from the $B$ Factories

## CP samples $\eta_f = -1$

- +  $B^0 \rightarrow J/\psi K_S^0 (\rightarrow \pi^+ \pi^-)$
- +  $B^0 \rightarrow J/\psi K_S^0 (\rightarrow \pi^0 \pi^0)$
- +  $B^0 \rightarrow \psi(2S) (\rightarrow \ell^+ \ell^-) K_S^0$
- +  $B^0 \rightarrow \psi(2S) (\rightarrow J/\psi \pi^+ \pi^-) K_S^0$
- +  $B^0 \rightarrow \chi_{c1} (\rightarrow J/\psi \gamma) K_S^0$
- +  $B^0 \rightarrow \eta_c (\rightarrow KK\pi) K_S^0$

## CP samples $\eta_f = +1$

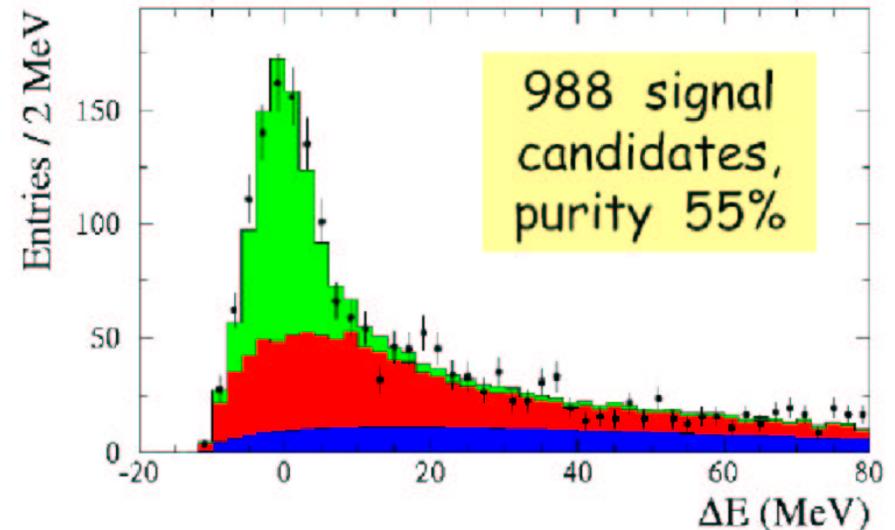
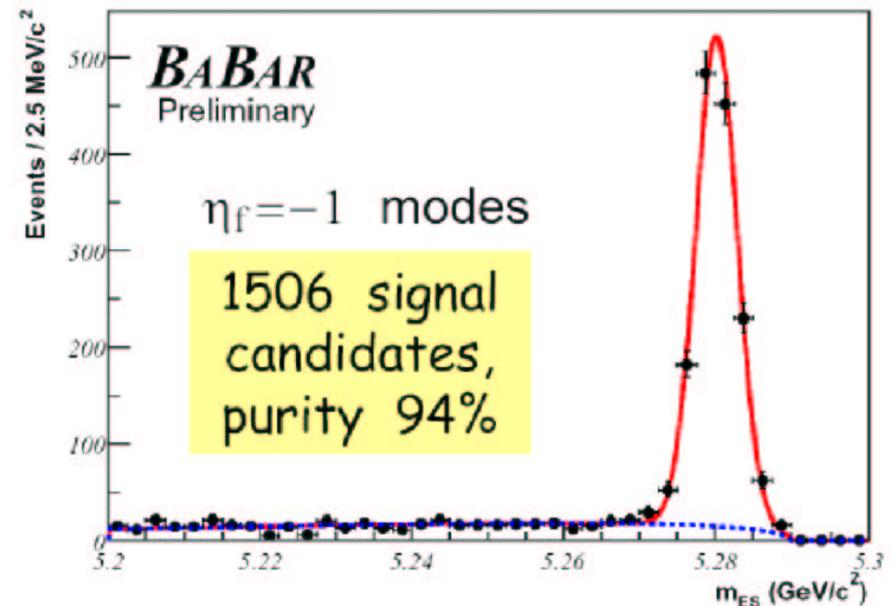
- +  $B^0 \rightarrow J/\psi K_L^0$

Integrated luminosity

Babar:  $81.3 \text{ fb}^{-1}$

Improved tagging:

$$\varepsilon D^2 = 28.1 \pm 0.7\%$$



# Asymmetries – Mixing and $CP$

---

Mixing asymmetry,  $\Delta m_d$

$$A_{mix}(t) \equiv \frac{N(t)_{unmix} - N(t)_{mix}}{N(t)_{unmix} + N(t)_{mix}} = D \cos(\Delta m_d t)$$

$CP$  asymmetry,  $\sin 2\beta$

$$A_{CP}(t) \equiv \frac{N(t)_{B^0 \rightarrow f_{CP}} - N(t)_{\overline{B^0} \rightarrow f_{CP}}}{N(t)_{B^0 \rightarrow f_{CP}} + N(t)_{\overline{B^0} \rightarrow f_{CP}}} = D \sin 2\beta \sin(\Delta m_q t)$$

Use large flavor sample to determine **dilution  $D$**  and **resolution functions**

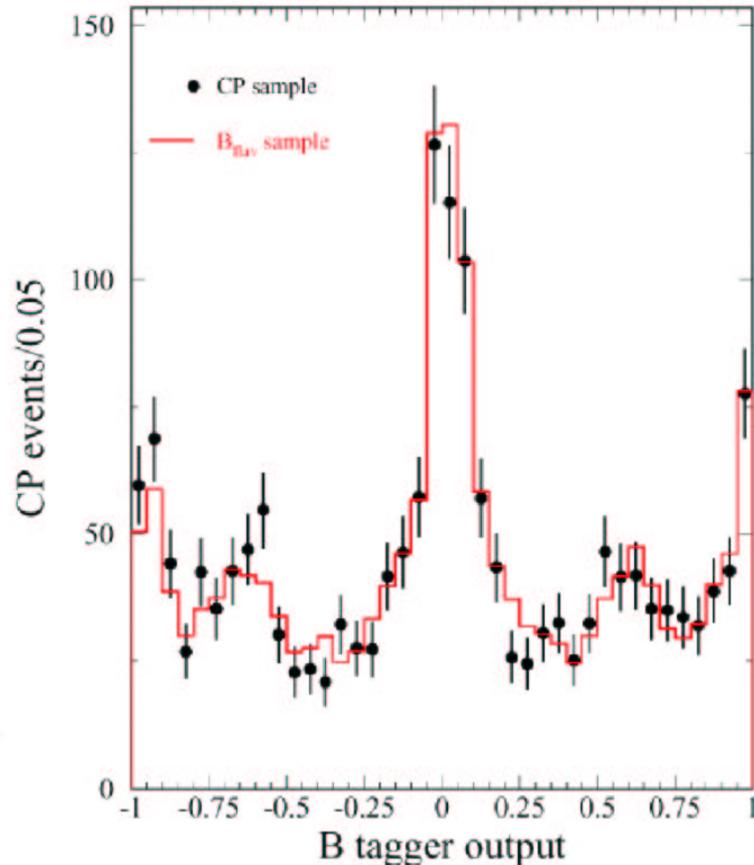
Transfer knowledge to significantly smaller  $CP$  sample

Same idea applies to Tevatron

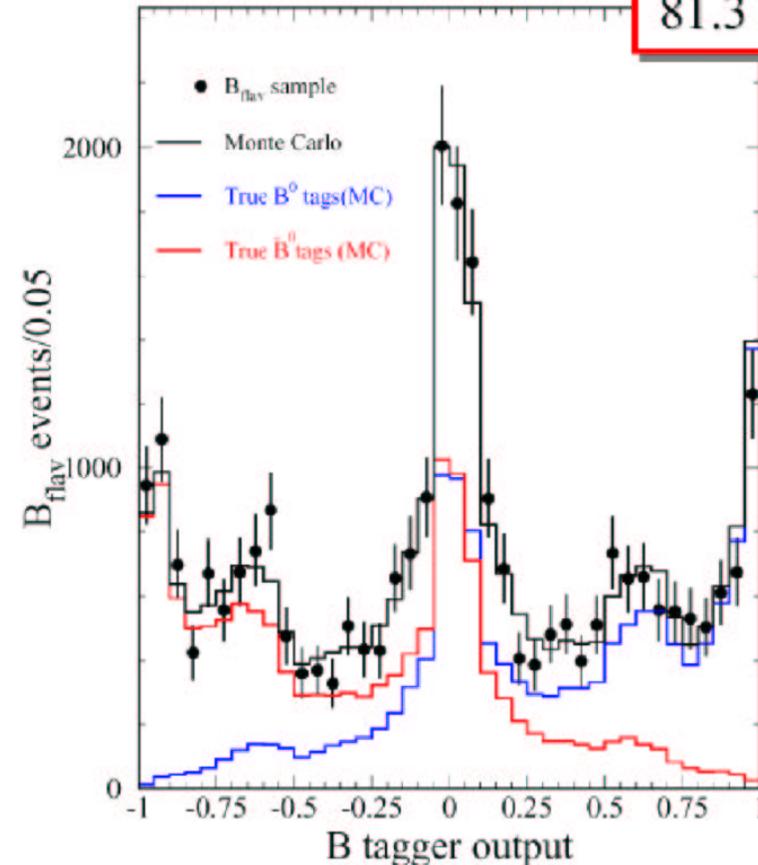
# Essential Tests of Taggers

**BABAR**

81.3 fb<sup>-1</sup>



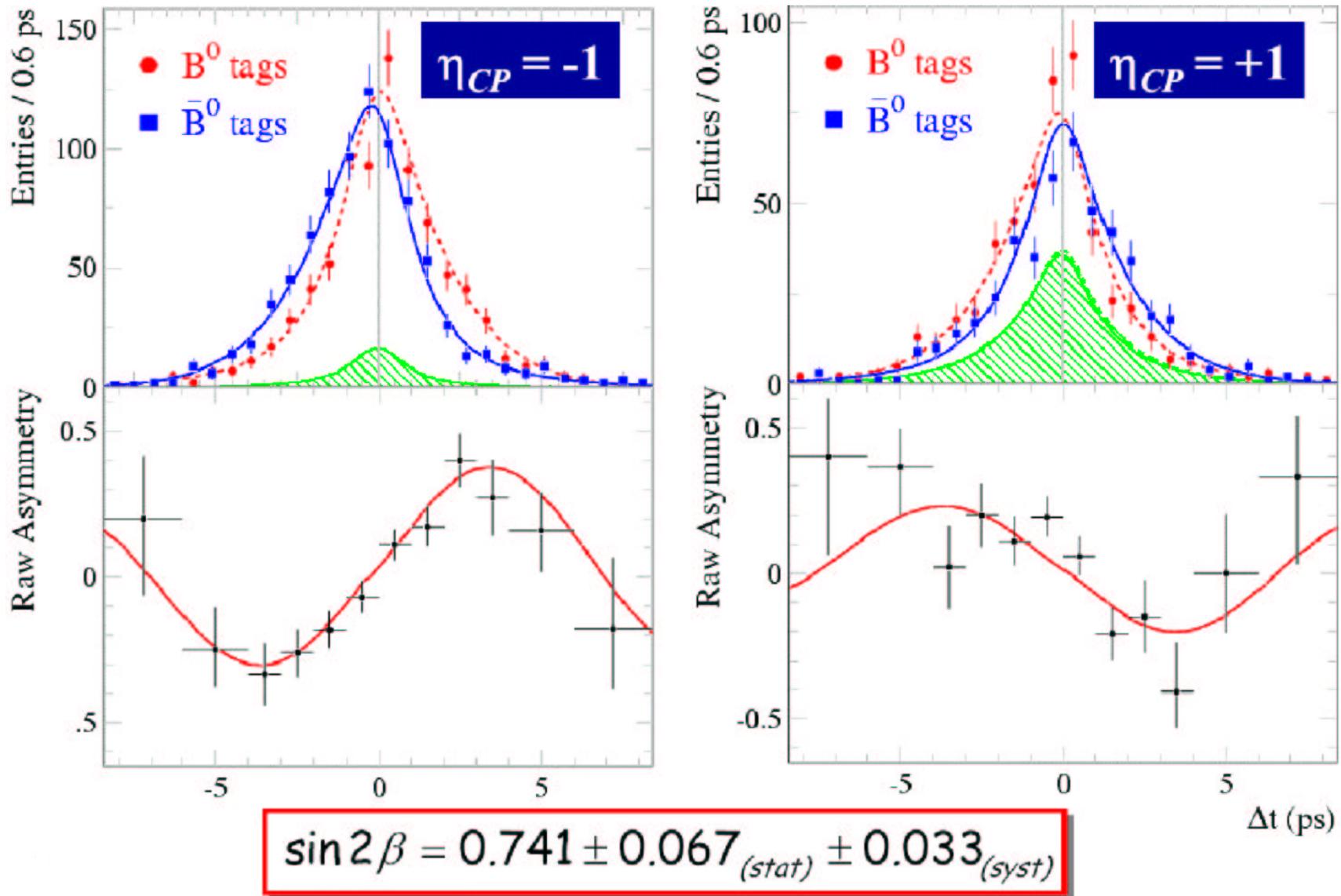
**CP vs  $B_{flav}$  sample**



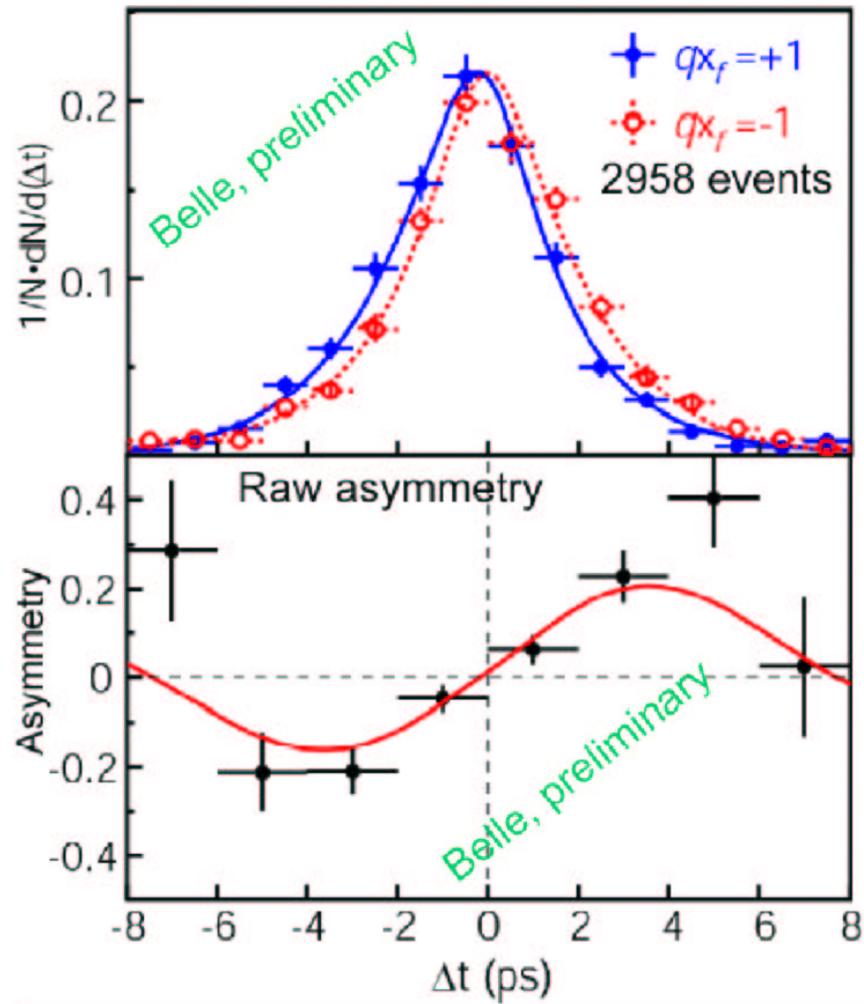
**$B_{flav}$  sample vs MC**

Crucial question: Does the tagger output look the same for the flavor and for the  $CP$  samples? **Yes it does!**

# BaBar Result for $\sin 2\beta$



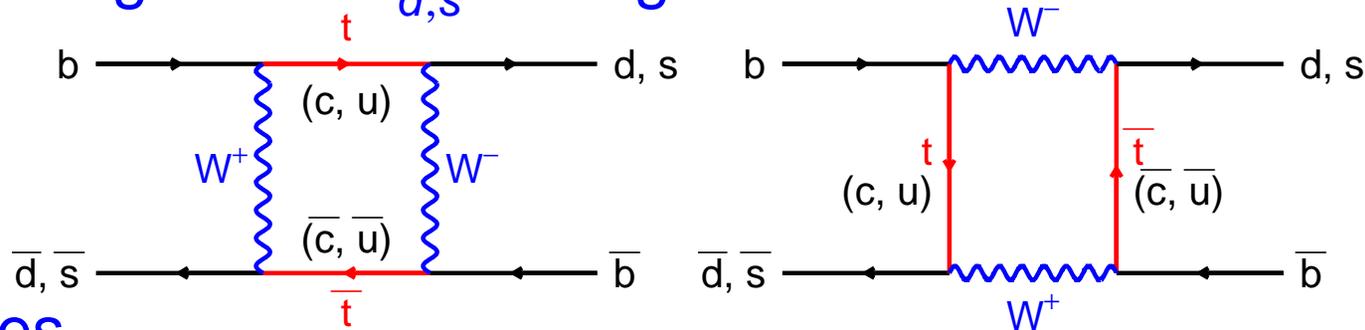
# Belle Result for $\sin 2\beta$



$$\sin 2\beta = 0.719 \pm 0.074_{(stat)} \pm 0.035_{(syst)}$$

# What is different for $B_s$ Mixing?

Feynman diagram of  $B_{d,s}^0$  mixing:

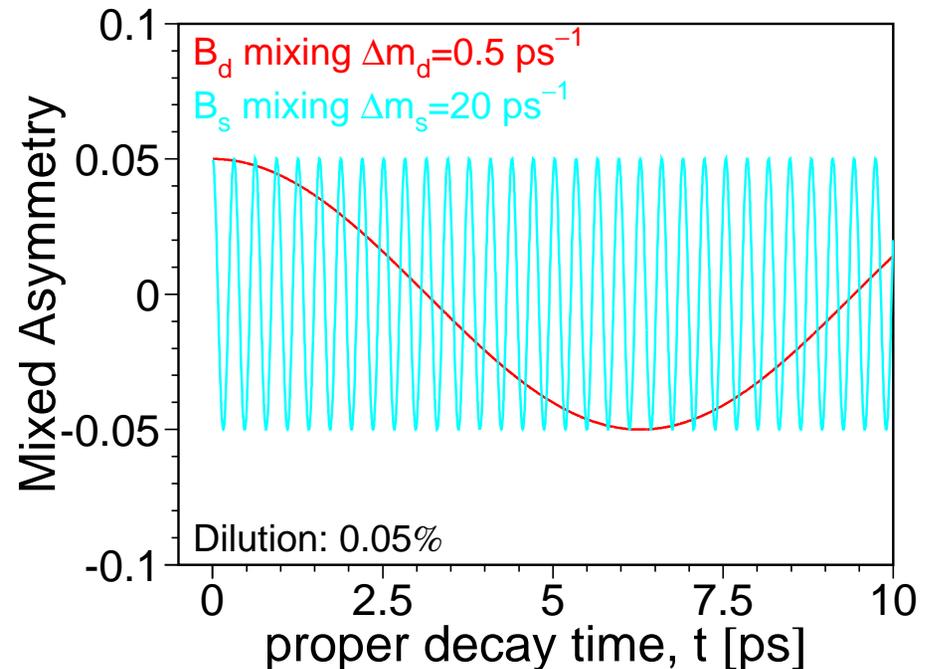


## Differences

- +  $B_d^0$  crosses two families
- +  $B_s^0$  crosses one family
- + faster  $B_s^0$  mixing ( $\approx 40$ )

## Experimental challenge

- +  $ct$  resolution critical
- + required resolution  $\approx 50$  fs
- + fully hadronic decays:  
 $B_s \rightarrow D_s^- \pi^+ (\pi^+ \pi^-)$
- + hadronic trigger (SVT)
- + Kaon identification (TOF)



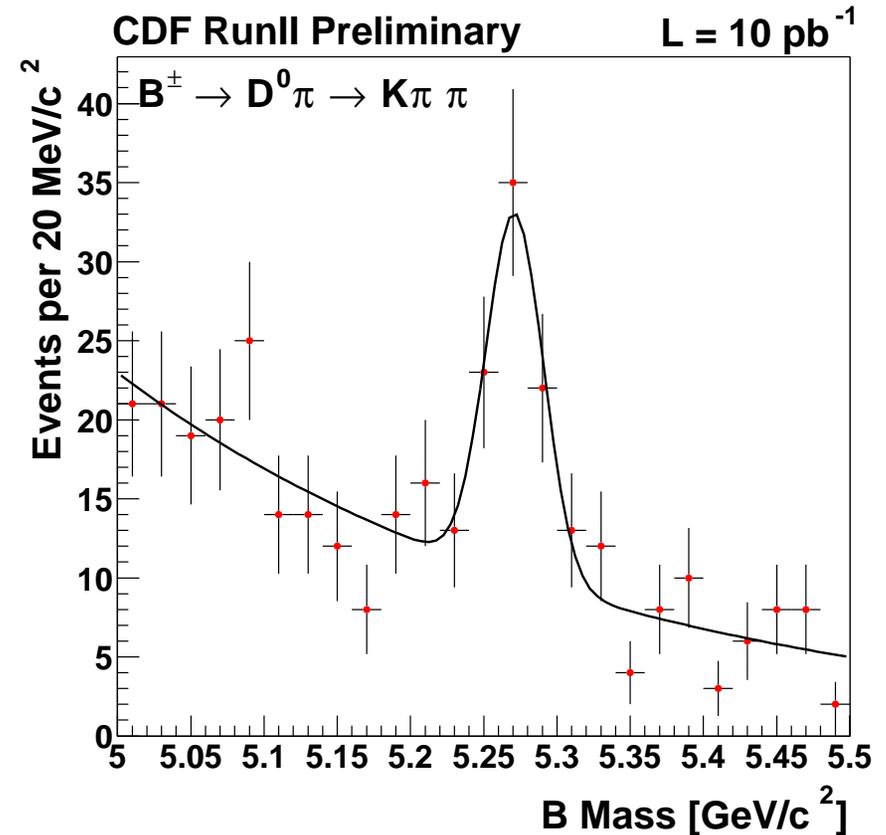
# Where are we in CDF with $B_s$ Mixing?

## Hadronic trigger

- + reasonably understood
- + reached design resolution  
 $\sigma(d_0) = 48 \mu\text{m}$
- + not as efficient as planned

## Offline tracking

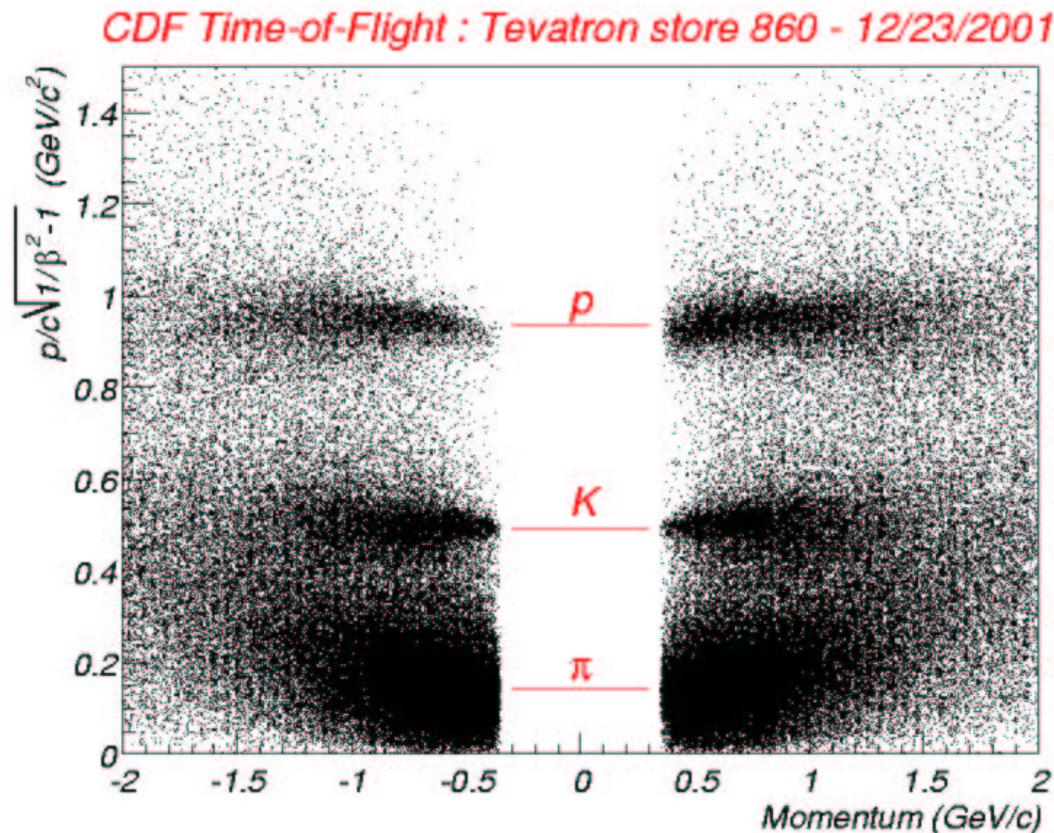
- +  $r$ - $\phi$  well understood
- +  $z$  tracking almost ready
- + essential L00 not yet used



# Where are we in CDF with $B_s$ Mixing?

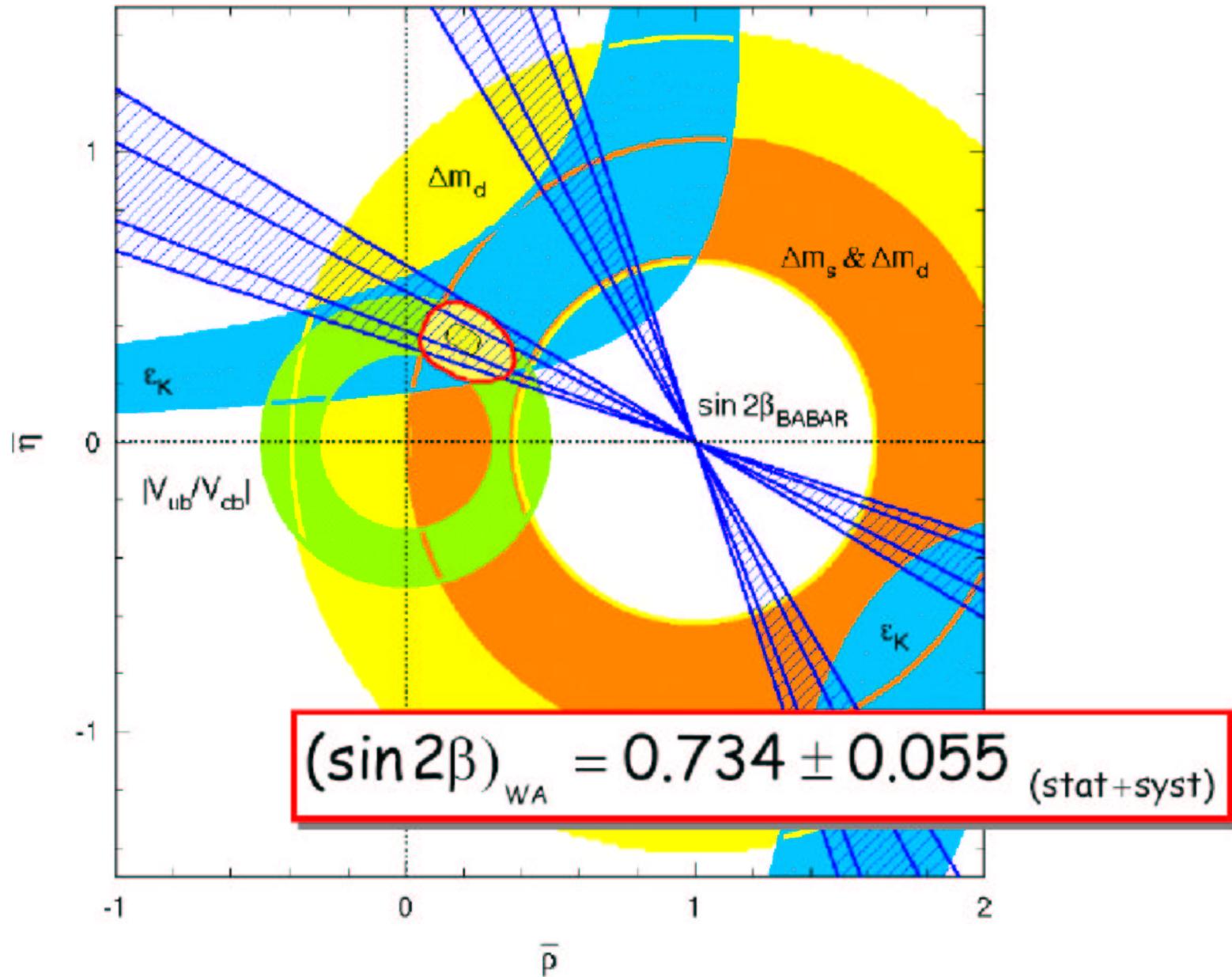
## Particle Id

- + TOF hardware works well; resolution per PMT as expected
- + efficiency lower than expected; too many hits per bar



First  $B_s$  mixing results not earlier than summer 2004

# Standard Model Constraints



# Conclusions

---

## Physics Motivation

- + *CKM* physics exciting: potential discrepancy with SM
- + amount of *CP* violation well predicted but too small
- + additional measurements test consistency of SM

## Comparison of $\Upsilon(4S)$ and $p\bar{p}$

- + beautifully complementary programs
- + high precision  $B^0, B^+$  at the *B* Factories
- + all other *b* hadrons at Tevatron

## Results

- + *CP* violation has been observed in *B* system
- + Era of precision *CKM* has started
- + consistent with expectations
- + lots of other *B* physics: spectroscopy  $B_s, B_c, \Lambda_b, B^{**}$  ..